

# **Radiative Neutrino Mass in light of the 750 GeV Diphoton Excess**

**Ivica Picek**  
**University of Zagreb**

**Oslo, 3 February 2016**

# SM Higgs Relatives:

## 1. Participating in EWSB

**Perturbative unitarity & Diphoton excess**

**M.Fabbrichesi, A.Urbano/1601.02447**

## 2. In Radiative Neutrino Models

**Without or with a loop/dark  $Z_2$  Symmetry**

**V.Brdar, IP, B.Radovčić, PLB 728 (2014) 198**

## 3. In Scotogenic Neutrino Models

**Derived dark  $Z_2$  Symmetry**

**E.Ma, IP, B.Radovčić, PLB 726 (2013) 744**

**Induced accidental  $Z_2$  Symmetry**

**P.Čuljak, IP, K.Kumerički, PLB 744 (2015) 237**

# 1. The SM Higgs: Now, Then & in Future

## 1.1 On July 4, 2012, we learned of the discovery of SM Higgs

- An excitation of a field that cooled with the rest of the universe underwent a condensation;
- Massive fields in SM acquire their masses from this condensate

Up Quark  
~ 0.002 GeV

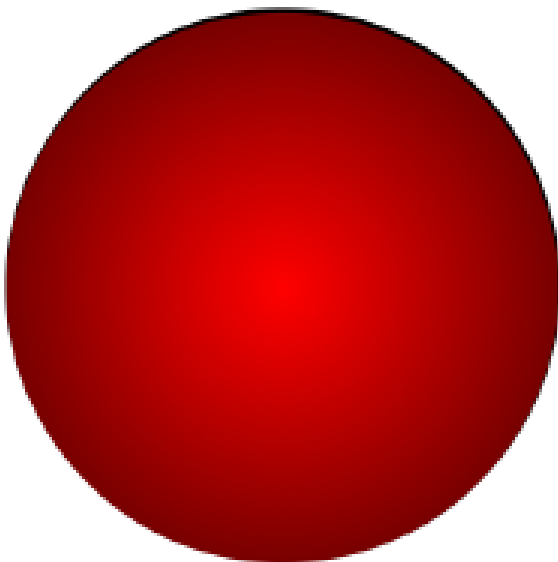
Charm Quark  
1.25 GeV

Top Quark  
175 GeV

Down Quark  
~ 0.005 GeV

Strange Quark  
~ 0.095 GeV

Bottom Quark  
4.2 GeV



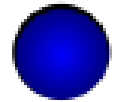
These are relative masses not size – they have no measurable size

Electron  
0.0005 GeV

Muon  
0.105 GeV

Tau  
1.78 GeV

For reference:



Proton  
0.938 GeV

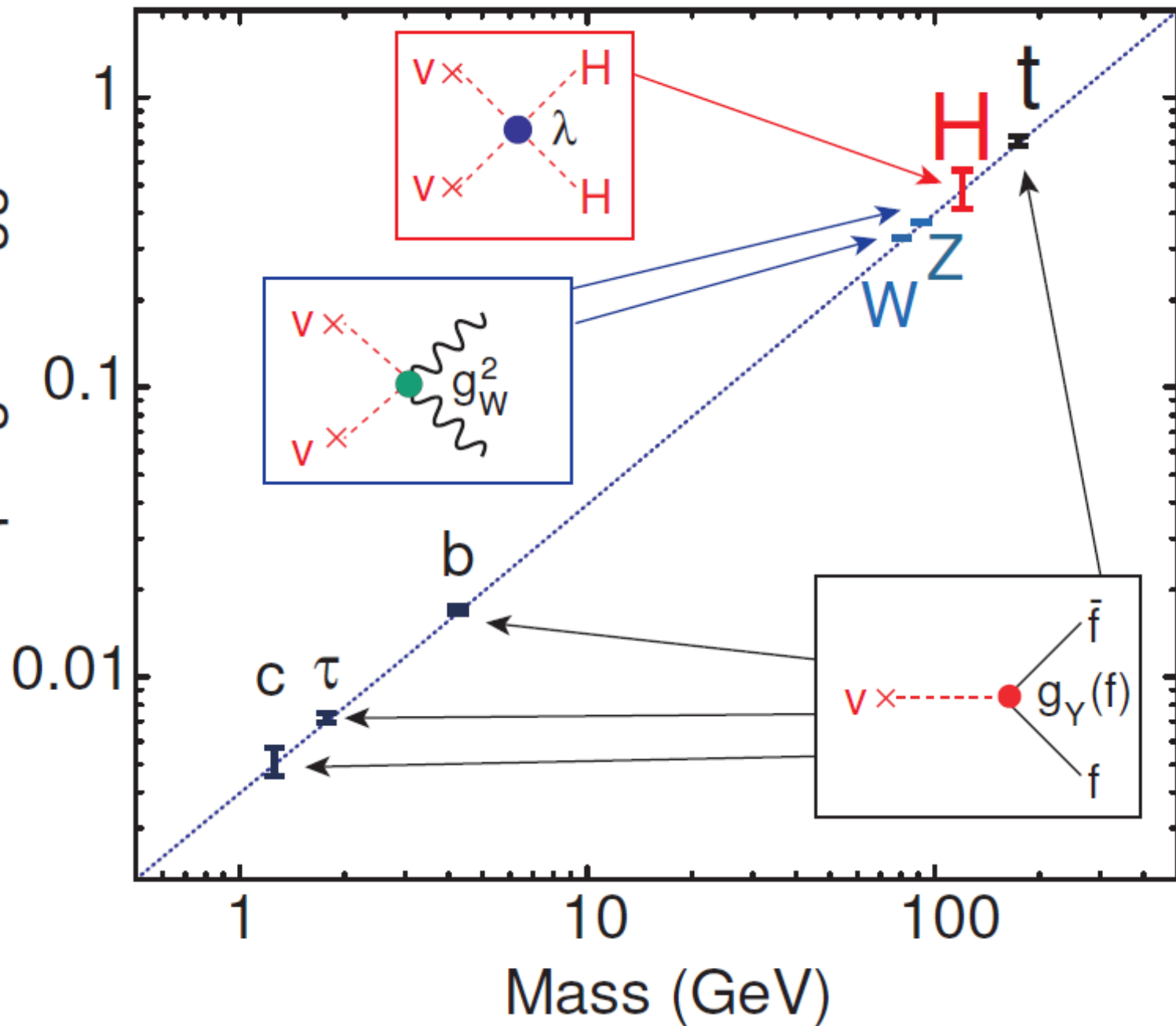
Electron Neutrino  
~ 0

Muon Neutrino  
~ 0

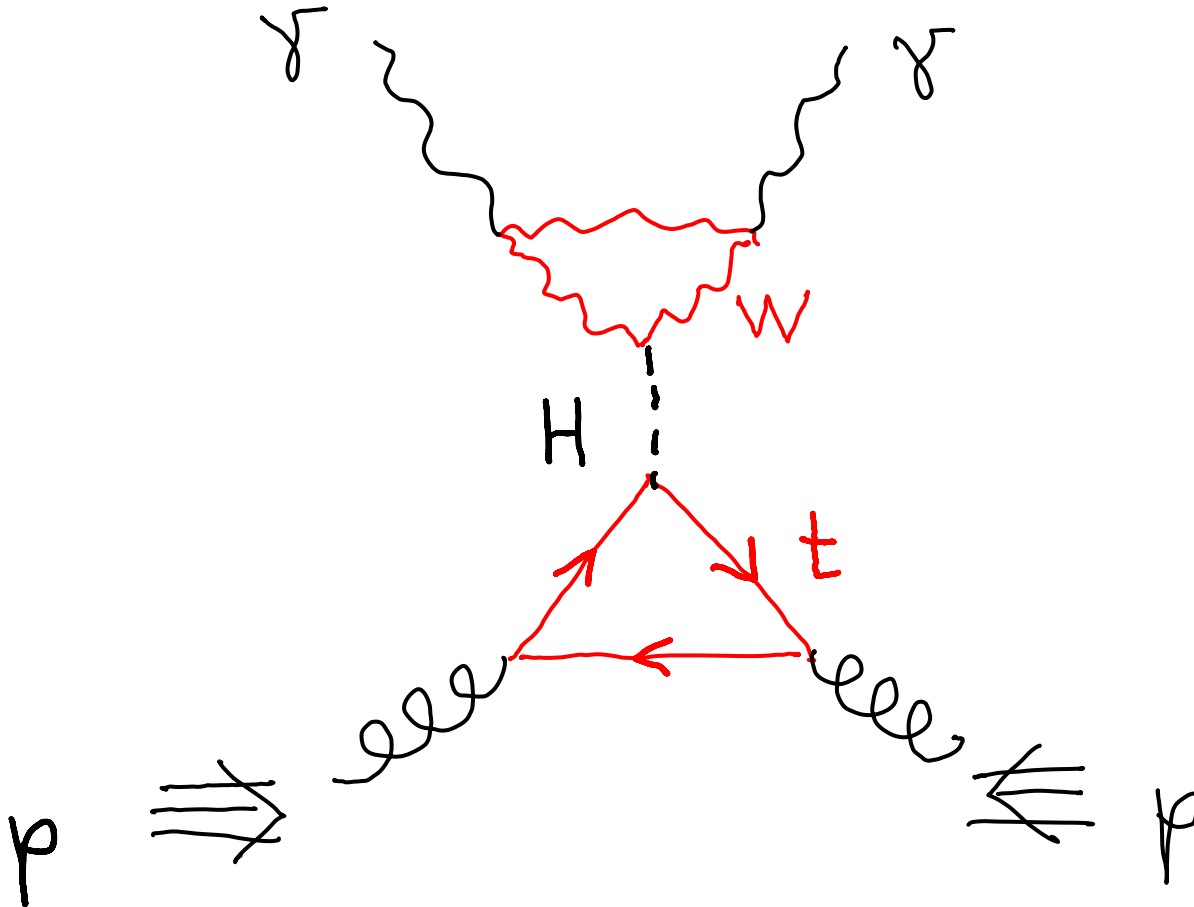
Tau Neutrino  
~ 0

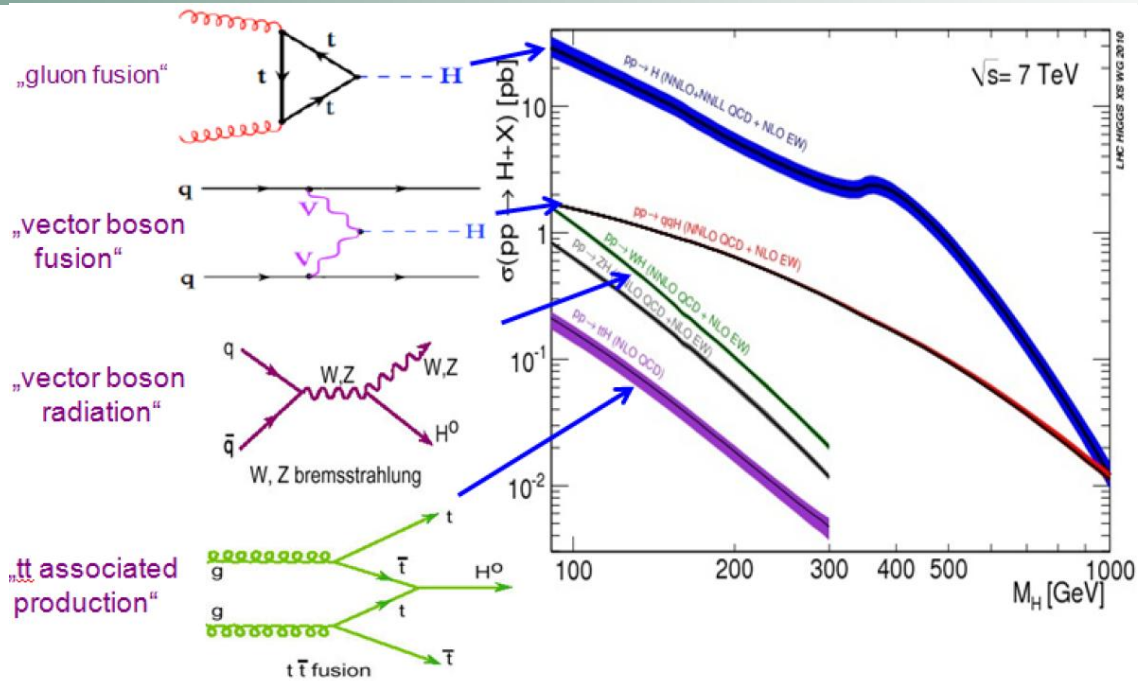
Originally thought to be massless but now not

Coupling to Higgs



# Pure Quantum- Discovery @ LHC: gluon fusion + rare decay

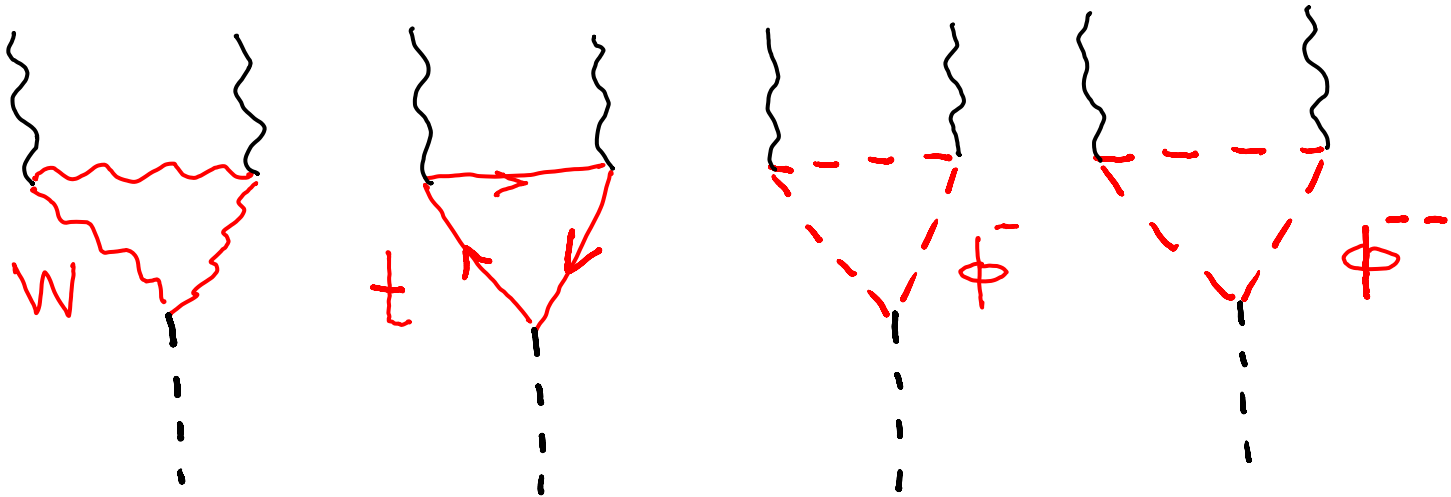




Decay mode	BR	Notes (as of early 2014)
$b\bar{b}$	58%	Observed at about $2\sigma$ at CMS
$WW^*$	22%	Observed at $4\sigma$
$gg$	8.6%	
$\tau\tau$	6.3%	Observed at $1-2\sigma$
$c\bar{c}$	2.9%	
$ZZ^*$	2.6%	Discovery mode (in $ZZ^* \rightarrow 4\mu, 2\mu 2e, 4e$ )
$\gamma\gamma$	0.23%	Discovery mode
$Z\gamma$	0.15%	
$\mu\mu$	0.022%	
$\Gamma_{\text{tot}}$	4.1 MeV	

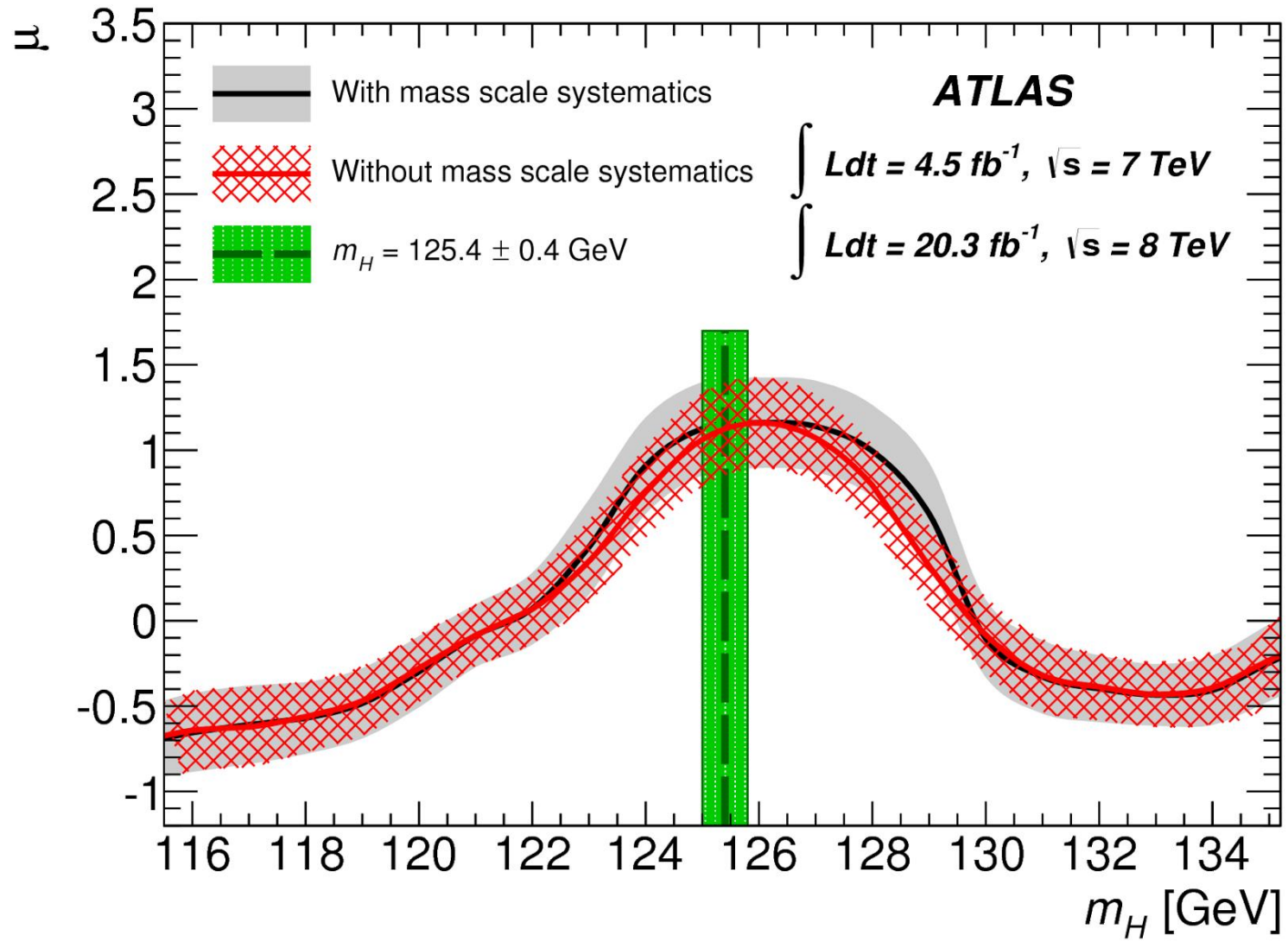
# BSM fields may give diphoton excess (important charged scalars)

$$\Gamma(h \rightarrow \gamma\gamma) = \frac{\alpha^2 m_h^3}{256\pi^3 v_H^2} \left| A_1(\tau_W) + N_c Q_t^2 A_{1/2}(\tau_t) + N_{c,S} Q_S^2 \frac{c_S}{2} \frac{v_H^2}{m_S^2} A_0(\tau_S) \right|^2$$





# No more Diphoton Excess at 125 GeV in 2014



# “The SM Periodic Table”

Three Generations  
of Matter (Fermions) spin  $\frac{1}{2}$

	I	II	III		
mass →	2.4 MeV	1.27 GeV	173.2 GeV	0	
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	
name →	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	
Quarks	4.8 MeV	104 MeV	4.2 GeV	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b><math>\gamma</math></b> photon	
Leptons	$0$	$0$	$0$	91.2 GeV	126 GeV
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino	0	0
	0.511 MeV	105.7 MeV	1.777 GeV	<b><math>Z^0</math></b> weak force	<b>H</b> Higgs boson
	-1	-1	-1	$\pm 1$	spin 0
	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau	<b><math>W^\pm</math></b> weak force	

Bosons (Forces) spin 1

# 1.2 Perturbative hints for the “BSM” discoveries in the past (dim 6 op's leading to $E^2$ scatt. ampl.)

- NP beyond the Fermi theory

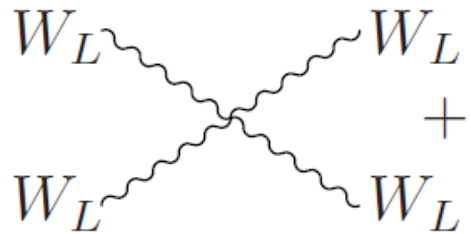
$$\sim G_F E^2 \simeq E^2 / v^2 < 16\pi^2 \longrightarrow m_W < 4\pi v$$

- The search for the top quark, because

$$\sim g_W^2 E^2 / m_W^2 < 16\pi^2 \longrightarrow m_t < 4\pi v$$

new theory must show up at an energy scale below  $4\pi/\sqrt{G_F} \simeq 4\pi v$ ,  
having expressed  $G_F = 1/\sqrt{2}v^2$  in terms of the EWSB scale  $v \simeq 246$  GeV.

The expectation of the Higgs, because of the quadratic term in the scatt. ampl.


$$+ \dots \sim g_W^2 E^2 / m_W^2 < 16\pi^2 \longrightarrow m_H < 4\pi v$$

the critical threshold of  $4\pi v \sim 3 \text{ TeV}$   
is within the reach of the LHC collider

Each time we replaced one d=6 operator  
with one new discovered state!

After discovering the Higgs we are left  
with genuinely g-inv ren-ble theory!

New physics is needed to explain Dark Matter,  
neutrino masses, Inflation and Baryogenesis

# 1.3 Only one Higgs doublet?

Difficult to imagine given the

- Huge disparity among SM fermion masses
- Lightness of neutrinos
- Fine tuning in the Higgs potential:

$$V = \text{const.} + m_H^2 |H|^2 + \lambda |H|^4$$

- Cosmological constant problem
- Higgs naturalness problem
- Vacuum stability problem

# Veltman parameter close to 1

$$\rho = \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} \quad \rho_{\text{exp}} = 1.0004^{+0.0003}_{-0.0004}$$

## ■ In extended Higgs sectors

$$\rho_{\text{tree}} = \frac{\sum_i [T_i(T_i + 1) - Y_i^2] v_i^2}{2 \sum_i Y_i^2 v_i^2}$$

## SM tree-value unchanged provided

$$T_i(T_i + 1) - 3Y_i^2 = 0$$

**Three main possibilities:** isospin singlets with  $Y_i = 0$ ,

doublets with  $Y_i = 1/2$ ,

and septets with  $Y_i = 2$

larger isospin representation fields

isospin 26-plet with  $Y_i = 15/2$

cause violation of perturbative unitarity

# Additional Complex Scalar Multiplet $X$

gauge-kinetic Lagrangian

$$\mathcal{L} \supset (\mathcal{D}_\mu \Phi)^\dagger (\mathcal{D}^\mu \Phi) + (\mathcal{D}_\mu X)^\dagger (\mathcal{D}^\mu X)$$

$$\mathcal{D}_\mu = \partial_\mu - ig' B_\mu Y - ig W_\mu^a T^a = \partial_\mu - ig' B_\mu Y - ig \left[ \frac{1}{2} (W_\mu^+ T^+ + W_\mu^- T^-) + W_\mu^3 T^3 \right]$$

■ **Masses for  $W$  and  $Z$**       the terms proportional to  $v_X^2$

$$(\mathcal{D}_\mu X)^\dagger (\mathcal{D}^\mu X) \supset X^\dagger \left[ \frac{g^2}{4} W_\mu^+ W^{-\mu} (T^+ T^- + T^- T^+) + g^2 W_\mu^3 W^{3\mu} (T^3)^2 + g'^2 B_\mu B^\mu (Y)^2 + 2gg' B_\mu W^{3\mu} (Y T^3) \right] X,$$

use  $Q = T^3 + Y$  so that  $T^3 = Q - Y = -Y$   
for the neutral component of  $X$  where the vev lives

# For a scalar $X$ of isospin $T$

$$\begin{aligned}T^+T^- + T^-T^+ &= \sqrt{2}(T^1 + iT^2)\sqrt{2}(T^1 - iT^2) + \sqrt{2}(T^1 - iT^2)\sqrt{2}(T^1 + iT^2) \\ &= 4 [(T^1)^2 + (T^2)^2] \\ &= 4 [|\vec{T}|^2 - (T^3)^2] \\ &= 4 [T(T+1) - (T^3)^2],\end{aligned}$$

■ Contributions - in convention

$$Q = T + Y$$

$$(\mathcal{D}_\mu X)^\dagger (\mathcal{D}^\mu X) \supset X^\dagger \left\{ g^2 W_\mu^+ W^{-\mu} [T(T+1) - Y^2] + g^2 W_\mu^3 W^{3\mu} (Y)^2 + g'^2 B_\mu B^\mu (Y)^2 - 2gg' B_\mu W^{3\mu} (Y)^2 \right\} X.$$

- ◇ Doublet,  $Y = 1/2$ :  $T(T+1) - Y^2 = \frac{1}{2}, \quad Y^2 = \frac{1}{4}.$
- ◇ Triplet,  $Y = 0$ :  $T(T+1) - Y^2 = 2, \quad Y^2 = 0.$
- ◇ Triplet,  $Y = 1$ :  $T(T+1) - Y^2 = 1, \quad Y^2 = 1.$



# 2. The 2HD Benchmark Model and Beyond

Theoretical problems of the SM

- Strong CP  $\bar{\theta} G^{\mu\nu} \tilde{G}_{\mu\nu} \quad (D = 4) \quad \longrightarrow \quad \bar{\theta} \lesssim 10^{-11}$
- EW naturalness  $\Lambda^2 H^\dagger H \quad (D = 2) \quad \longrightarrow \quad \Lambda \approx 100 \text{ GeV}$
- Cosmological constant  $\Lambda^4 \sqrt{g} \quad (D = 0) \quad \longrightarrow \quad \Lambda \approx 10^{-3} \text{ eV}$
- Landau poles
- ...

- Evidence/hints for physics beyond the SM

- Neutrino oscillations
- Dark Matter
- Baryon asymmetry
- EW vacuum instability
- Gravity



A simple scalar extension of the SM may account for all these issues

# 2.1 Simplest scalar extensions

**i) Real triplet**  
**T=1, Y=0 (VEV):**

$$\Xi = \begin{pmatrix} \xi^+ \\ \xi^0 \\ \xi^- \end{pmatrix} \rightarrow \begin{pmatrix} \xi^+ \\ \xi^0 + v_\xi \\ \xi^- \end{pmatrix}$$

$$\frac{1}{2}(\mathcal{D}_\mu \Xi)^\dagger (\mathcal{D}^\mu \Xi) \supset g^2 v_\xi^2 W_\mu^+ W^{-\mu}$$

$$\langle \Xi \rangle = \begin{pmatrix} 0 \\ v_\xi \\ 0 \end{pmatrix}$$

■ **Y=0, so no contribution to neutral boson masses**

$$M_{\Xi}^2 = v_\xi^2 \begin{pmatrix} g^2 & 0 & 0 & 0 \\ 0 & g^2 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

## ii) Complex triplet

**T=1, Y=1 (VEV):**

$$\langle X \rangle = \begin{pmatrix} 0 \\ 0 \\ v_\chi \end{pmatrix}$$

$$X = \begin{pmatrix} \chi^{++} \\ \chi^+ \\ \chi^0 \end{pmatrix} \rightarrow \begin{pmatrix} \chi^{++} \\ \chi^+ \\ v_\chi + (h_\chi + ia_\chi)/\sqrt{2} \end{pmatrix}$$

$$(\mathcal{D}_\mu X)^\dagger (\mathcal{D}^\mu X) \supset g^2 v_\chi^2 W_\mu^+ W^{-\mu} + g^2 v_\chi^2 W_\mu^3 W^{3\mu} + g'^2 v_\chi^2 B_\mu B^\mu - 2gg' v_\chi^2 B_\mu W^{3\mu}$$

### ■ Mass-square contributions for W i Z

$$M_X^2 = v_\chi^2 \begin{pmatrix} g^2 & 0 & 0 & 0 \\ 0 & g^2 & 0 & 0 \\ 0 & 0 & 2g^2 & -2gg' \\ 0 & 0 & -2gg' & 2g'^2 \end{pmatrix}$$

the lower  $2 \times 2$  block of this matrix is still diagonalized by the same weak mixing angle  $\theta_W$

does not generate the same masses for the  $W$  and  $Z$  in the limit  $g' \rightarrow 0$

# Custodial symm. restoration for both triplets, $Y=0$ & $Y=1$

$$M_W^2 = \frac{g^2}{4}(v_\phi^2 + 4v_\xi^2 + 4v_\chi^2)$$

$$M_Z^2 = \frac{g^2 + g'^2}{4}(v_\phi^2 + 8v_\chi^2) = \frac{g^2}{4c_W^2}(v_\phi^2 + 8v_\chi^2)$$

$$\rho \equiv \frac{M_W^2}{c_W^2 M_Z^2} = \frac{v_\phi^2 + 4v_\xi^2 + 4v_\chi^2}{v_\phi^2 + 8v_\chi^2}$$

- The rho parameter tuned to 1 for aligned

$$v_\xi = v_\chi \equiv v_3$$

$$M_{X+\Xi}^2 = 2v_3^2 \begin{pmatrix} g^2 & 0 & 0 & 0 \\ 0 & g^2 & 0 & 0 \\ 0 & 0 & g^2 & -gg' \\ 0 & 0 & -gg' & g'^2 \end{pmatrix}$$

the rotation symmetry

The custodial SU(2) symmetry is restored:  $W^1 \leftrightarrow W^2 \leftrightarrow W^3$

in the limit  $g' \rightarrow 0$ , the  $W$  and  $Z$  masses again become equal

# Georgi-Machacek model with bidoublet-like 3x3 object

- containing both triplets  $Y=1$  &  $Y=0$

to engineer the relationship  $v_\xi = v_\chi$

$$\langle \tilde{X} \rangle = \begin{pmatrix} v_\chi & 0 & 0 \\ 0 & v_\chi & 0 \\ 0 & 0 & v_\chi \end{pmatrix}$$
$$\tilde{X} = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ \chi^- & \xi^0 & \chi^+ \\ \chi^{--} & \xi^- & \chi^0 \end{pmatrix} \quad \text{where } \chi^- = -\chi^{+*} \text{ and } \xi^- = -\xi^{+*}$$

transforms as a triplet under both the global  $SU(2)_L$  and  $SU(2)_R$

by allowing an alignment among VEVs, we can keep  $\rho_{\text{tree}} = 1$

■ **If this is symmetry of the scalar potential**

the resulting model is called the Georgi-Machacek model

“Doubly Charged Higgs Bosons,”  
Nucl. Phys. B **262**, 463 (1985)

## 2.2 Two Higgs Doublet - 2HDM

the most explored benchmark model

$$\Phi_1 = \begin{pmatrix} \phi_1^+ \\ (h_1 + v_1 + ia_1)/\sqrt{2} \end{pmatrix}, \quad \Phi_2 = \begin{pmatrix} \phi_2^+ \\ (h_2 + v_2 + ia_2)/\sqrt{2} \end{pmatrix}$$

- Both fields participate in EWSB
- Real VEVs avoid CPV in scalar sector
- Can provide a custodial singlet with the couplings to  $g_b$  fixed by  $g$ -invariance, to cancel the unitarity growth

# Most general non-SuSy 2HDM with CP conserving potential

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} (G^+ \cos \beta - H^+ \sin \beta) \\ v_1 - h \sin \alpha + H \cos \alpha + i (G \cos \beta - A \sin \beta) \end{pmatrix}$$

$$\Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} (G^+ \sin \beta + H^+ \cos \beta) \\ v_2 + h \cos \alpha + H \sin \alpha + i (G \sin \beta + A \cos \beta) \end{pmatrix}$$

$$\begin{aligned} \mathcal{V}_{2\text{HDM}} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - [m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}] \\ & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) \\ & + \left\{ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + [\lambda_6 (\Phi_1^\dagger \Phi_1) + \lambda_7 (\Phi_2^\dagger \Phi_2)] \Phi_1^\dagger \Phi_2 + \text{h.c.} \right\}. \end{aligned}$$

■ **To avoid FCNC (with “natural flavor cons”)**

impose a  $Z_2$  symmetry so that each type of fermion only couples to one of the doublets

(forcing  $\lambda_6 = \lambda_7 = 0$ )

# Natural Flavor Conservation NFC

- **Type I:**  $u_R, d_R, e_R \rightarrow -u_R, -d_R, -e_R$
- **Type II:**  $u_R \rightarrow -u_R$  and  $d_R, e_R \rightarrow d_R, e_R$
- **Type X** (lepton specific):  $u_R, d_R \rightarrow -u_R, -d_R$  and  $e_R \rightarrow e_R$
- **Type Y** (flipped):  $u_R, e_R \rightarrow -u_R, -e_R$  and  $d_R \rightarrow d_R$

TABLE I. Four types of the charge assignment of the  $Z_2$  symmetry.

	$\Phi_1$	$\Phi_2$	$u_R$	$d_R$	$\ell_R$	$Q_L, L_L$
Type-I	+	-	-	-	-	+
Type-II	+	-	-	+	+	+
Type-X	+	-	-	-	+	+
Type-Y	+	-	-	+	-	+



**2.3 Custodial Triplet (GMM)**  
contains a singlet resonance that  
can take part in EWSB and still  
belong to a perturbative regime

$$\Phi_{(2,2)} \equiv \begin{pmatrix} \phi^{0*} & \phi^+ \\ \phi^- & \phi^0 \end{pmatrix}, \quad \Delta_{(3,3)} \equiv \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ \chi^- & \xi^0 & \chi^+ \\ \chi^{--} & \xi^- & \chi^0 \end{pmatrix}$$

whose VEVs are

$$\langle \Phi \rangle = \frac{v_\phi}{\sqrt{2}} \hat{I}_{2 \times 2} \quad \text{and} \quad \langle \Delta \rangle = \frac{v_\Delta}{\sqrt{2}} \hat{I}_{3 \times 3}$$

$$\text{with } v_\phi^2 + 8v_\Delta^2 = v^2 = 1/\sqrt{2} G_F \simeq (246 \text{ GeV})^2$$

- C-W Chiang, A-L Kuo/1601.06394 **fit the 750 diphoton resonance with the Singlet of Custodial Triplet Model**

$$\Phi = \begin{pmatrix} \phi^{0*} & \phi^+ \\ -\phi^- & \phi^0 \end{pmatrix}, \quad \Delta = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ -\chi^- & \xi^0 & \chi^+ \\ \chi^{--} & -\xi^- & \chi^0 \end{pmatrix}$$

$$\begin{aligned} V = & \frac{1}{2}m_1^2 \text{tr}[\Phi^\dagger\Phi] + \frac{1}{2}m_2^2 \text{tr}[\Delta^\dagger\Delta] + \lambda_1 (\text{tr}[\Phi^\dagger\Phi])^2 + \lambda_2 (\text{tr}[\Delta^\dagger\Delta])^2 \\ & + \lambda_3 \text{tr} [(\Delta^\dagger\Delta)^2] + \lambda_4 \text{tr}[\Phi^\dagger\Phi] \text{tr}[\Delta^\dagger\Delta] + \lambda_5 \text{tr} \left[ \Phi^\dagger \frac{\sigma^a}{2} \Phi \frac{\sigma^b}{2} \right] \text{tr}[\Delta^\dagger T^a \Delta T^b] \\ & + \mu_1 \text{tr} \left[ \Phi^\dagger \frac{\sigma^a}{2} \Phi \frac{\sigma^b}{2} \right] (P^\dagger \Delta P)_{ab} + \mu_2 \text{tr}[\Delta^\dagger T^a \Delta T^b] (P^\dagger \Delta P)_{ab}, \end{aligned}$$

$$P = \frac{1}{\sqrt{2}} \begin{pmatrix} -1 & i & 0 \\ 0 & 0 & \sqrt{2} \\ 1 & i & 0 \end{pmatrix}$$

**diagonalizes the adjoint rep of SU(2)**

# 10 phys. states among 13 rep's under $SU(2)$ -custodial

$$(\mathbf{2}, \mathbf{2}) \sim \mathbf{1} \oplus \mathbf{3}, \text{ and } (\mathbf{3}, \mathbf{3}) \sim \mathbf{1} \oplus \mathbf{3} \oplus \mathbf{5}$$

$SU(2)_C$  singlets  $H_1^0, H_1^{0'}$  (the Higgs and the additional resonance)

one  $SU(2)_C$  triplet  $(H_3^+, H_3^0, H_3^-)$

one  $SU(2)_C$  quintuplet  $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$

- Fabbrichesi-Urbano/1601.02447 fit the 750 diphoton resonance with the physical “additional resonance”

$$H = s_\alpha H_1^0 + c_\alpha H_1^{0'}$$

# 3. The Resonance at 750 GeV that Stole Christmas

- the title of N. Craig et al./1512.04928

The ATLAS announcement [1] of a  $3.6\sigma$  local excess in diphotons with invariant masses near  $m_{\gamma\gamma} \sim 750$  GeV

$$\sigma(pp \rightarrow \phi \rightarrow \gamma\gamma) = (6.2_{-2.0}^{+2.4}) \text{ fb} \quad (\text{ATLAS})$$

$$= (5.6 \pm 2.4) \text{ fb} \quad (\text{CMS})$$

$$\Gamma_{\text{tot}}(\phi) \sim 45 \text{ GeV} (\text{ATLAS})$$

[1] The ATLAS collaboration, ATLAS-CONF-2015-081.

[2] CMS Collaboration [CMS Collaboration], collisions at 13TeV," CMS-PAS-EXO-15-004.

# 3.1 Fitting the 750 GeV state

## ■ **M.R. Buckley/1601.04751**

as a follow-up to the work of Refs. [4–6], which have largely set the parameters which later papers have adopted

## ■ **The most statistically significant deviation from the SM at the LHC made public since the discovery of the Higgs boson at 125 GeV**

[4] S. Knapen, T. Melia, M. Papucci and K. Zurek, arXiv:1512.04928 [hep-ph].

[5] R. S. Gupta, S. Jger, Y. Kats, G. Perez and E. Stamou, arXiv:1512.05332 [hep-ph].

[6] A. Falkowski, O. Slone and T. Volansky, arXiv:1512.05777 [hep-ph].

# A hint of a second scalar boson like in Radiative Neutrino Models

- 2HDMs cannot accommodate without additional massive particles

A. Angelescu, A. Djouadi and G. Moreau, *Scenarii for interpretations of the LHC diphoton excess: two Higgs doublets and vector-like quarks and leptons*, [arXiv:1512.04921[hep-ph]]. 2

W. Altmannshofer, J. Galloway, S. Gori, A. L. Kagan, A. Martin and J. Zupan, *On the 750 GeV di-photon excess*, [arXiv:1512.07616[hep-ph]].

- A need to go beyond purely scalar explanations

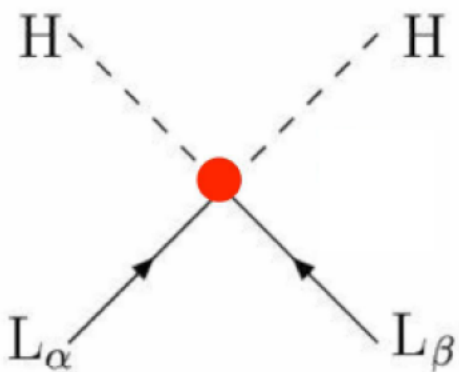
C. W. Murphy, *Vector Leptoquarks and the 750 GeV Diphoton Resonance at the LHC*, [arXiv:1512.06976[hep-ph]]. 2

# 3.2 Radiative Neutrino Models

Integrating out BSM particles produces an effective Dim 5 neutrino-mass operator

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{\lambda}{M} \underbrace{\bar{L} \tilde{H} \tilde{H}^T L^c}_{\text{dim-5}} + O\left(\frac{1}{M^2}\right)$$

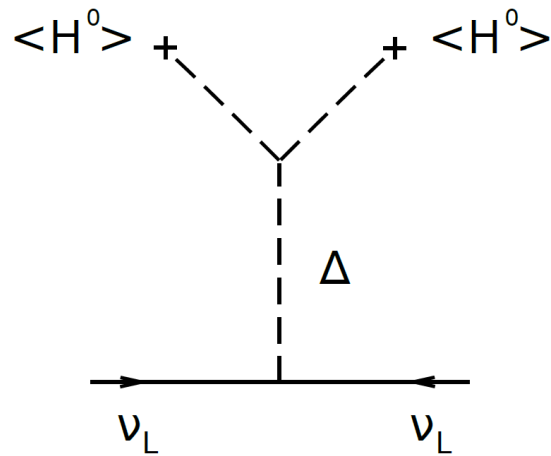
$L_L$  — lepton doublet  
 $H$  — Higgs boson doublet  
 $M$  — heavy mass



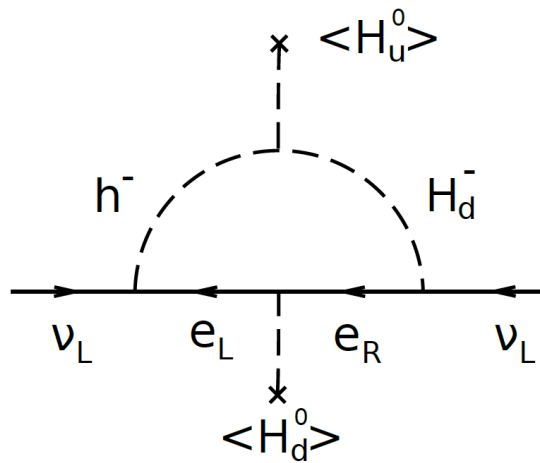
$$\langle H \rangle_0 = v \quad \longrightarrow \quad m_\nu \sim \lambda v \left( \frac{v}{M} \right)$$

# Dim 5 op. in scalar extensions: weak triplet w.r.t. 2nd doublet + charged scalars @ loop level

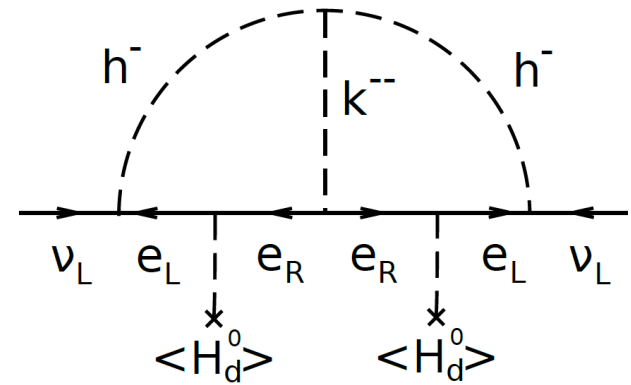
$$(llHH)/\Lambda$$



$$(llle^c H)/\Lambda^3$$



$$(llle^c le^c)/\Lambda^5$$



[Schechter, Valle (1980),  
Cheng, Li (1980),  
Lazarides, Shafi, Wetterich (1981),  
Mohapatra, Senjanovic (1981)]

[Zee (1980), Wolfenstein (1980),  
Babu, Julio (2014)]

[Zee (1986), Babu (1988)]



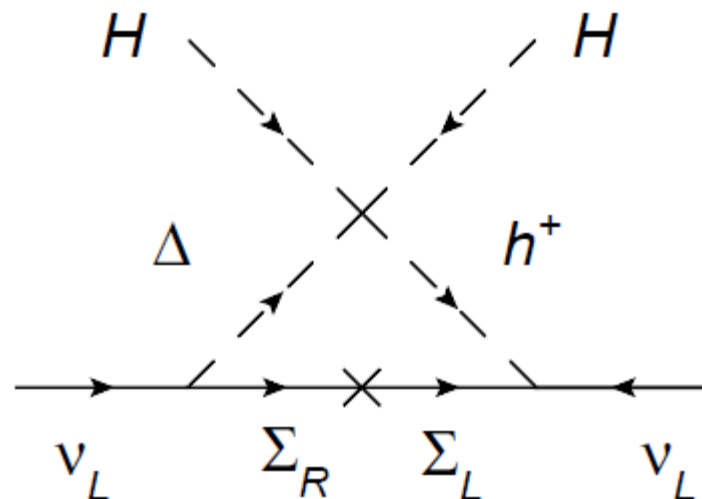
# Radiative mass with real ( $Y=0$ ) Triplet Scalar

BPR, PLB 728 (2014) 198

$$\Delta = \frac{1}{\sqrt{2}} \sum_j \sigma_j \Delta^j = \begin{pmatrix} \frac{1}{\sqrt{2}} \Delta^0 & \Delta^+ \\ \Delta^- & -\frac{1}{\sqrt{2}} \Delta^0 \end{pmatrix} \sim (3, 0)$$

- Additional charged scalar singlet  $h^+ \sim (1, 2)$
- Additional vectorlike lepton doublet

$$\Sigma_R \equiv (\Sigma_R^0, \Sigma_R^-)^T \sim (2, -1), \quad \Sigma_L \equiv (\Sigma_L^0, \Sigma_L^-)^T \sim (2, -1)$$



## ■ Gauge invariant scalar potential

$$\begin{aligned}
 V(H, \Delta, h^+) = & -\mu_H^2 H^\dagger H + \lambda_1 (H^\dagger H)^2 + \mu_h^2 h^- h^+ + \lambda_2 (h^- h^+)^2 \\
 & + \mu_\Delta^2 \text{Tr}[\Delta^2] + \lambda_3 (\text{Tr}[\Delta^2])^2 + \lambda_4 H^\dagger H h^- h^+ + \lambda_5 H^\dagger H \text{Tr}[\Delta^2] \\
 & + \lambda_6 h^- h^+ \text{Tr}[\Delta^2] + (\lambda_7 H^\dagger \Delta \tilde{H} h^+ + \text{H.c.}) + \mu H^\dagger \Delta H .
 \end{aligned}$$

## ■ The neutrino mass matrix

$$\begin{aligned}
 \mathcal{M}_{ij} = & \sum_{k=1}^3 \frac{[(g_1)_{ik}(g_2)_{jk} + (g_2)_{ik}(g_1)_{jk}]}{8\pi^2} \lambda_7 v_H^2 M_{\Sigma_k} \\
 & \frac{M_{\Sigma_k}^2 m_{h^+}^2 \ln \frac{M_{\Sigma_k}^2}{m_{h^+}^2} + M_{\Sigma_k}^2 m_{\Delta^+}^2 \ln \frac{m_{\Delta^+}^2}{M_{\Sigma_k}^2} + m_{h^+}^2 m_{\Delta^+}^2 \ln \frac{m_{h^+}^2}{m_{\Delta^+}^2}}{(m_{h^+}^2 - m_{\Delta^+}^2)(M_{\Sigma_k}^2 - m_{h^+}^2)(M_{\Sigma_k}^2 - m_{\Delta^+}^2)}
 \end{aligned}$$

# 3.3 Inert-Scotogenic variants

## - as a link to DM problem

### ■ Scotogenic model with $Z_2$ symmetry

V.Brdar, IP, B.Radovčić, PLB 728 (2014) 198

$$\begin{pmatrix} h^- & \Delta^- \end{pmatrix} \begin{pmatrix} \mu_h^2 + \lambda_4 v_H^2 & \lambda_7 v_H^2 \\ \lambda_7 v_H^2 & \mu_\Delta^2 + 2\lambda_5 v_H^2 \end{pmatrix} \begin{pmatrix} h^+ \\ \Delta^+ \end{pmatrix}$$

relation to the mass eigenstates is given by

$$\begin{pmatrix} h^+ \\ \Delta^+ \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} S_1^+ \\ S_2^+ \end{pmatrix}.$$

### ■ Scotogenic model with $U(1)_D$ gauge symm.

E.Ma, IP, B.Radovčić, PLB 726 (2013) 744

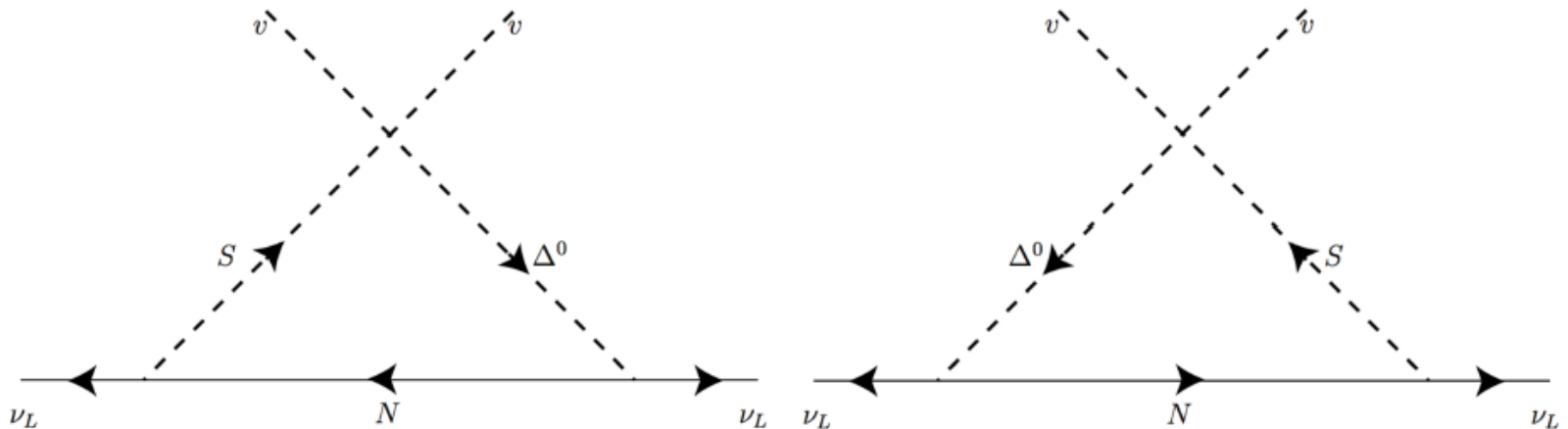
$$\Delta V(H, \Delta) = \lambda_8 (\Delta^\dagger \tau_a^{(3)} \Delta)^2 + \lambda_9 (H^\dagger \tau_a^{(2)} H) (\Delta^\dagger \tau_a^{(3)} \Delta)$$

# Radiative mass with $Y=2$ Inert Triplet Scalar

## Particle content

H.Okada, Y.Orikasa:  
1512.06687

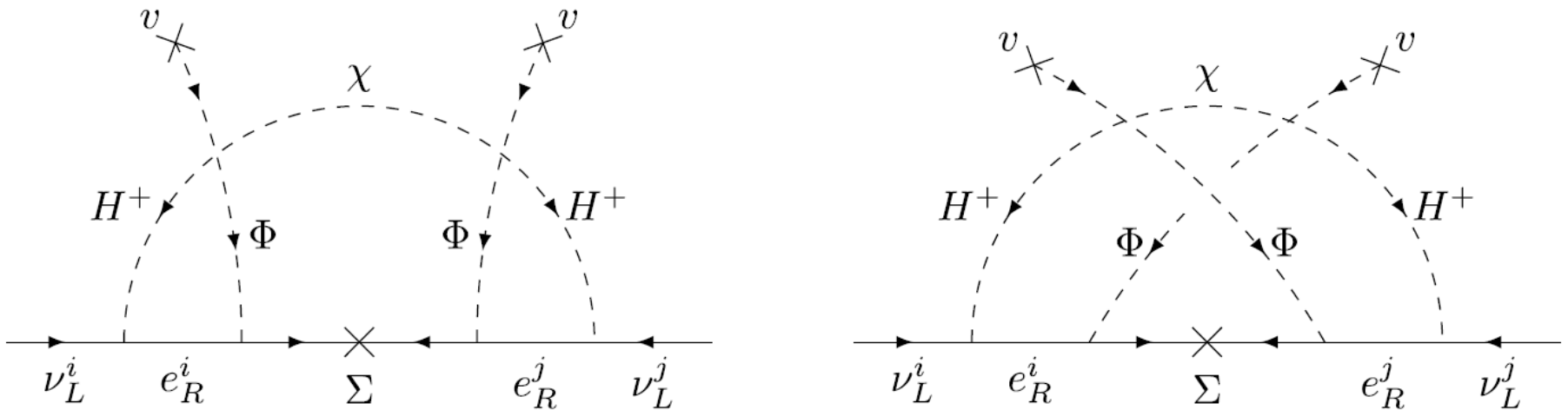
	Lepton Fields			Scalar Fields		
	$L_L$	$e_R$	$L'$	$\Phi$	$\Delta$	$S$
$SU(2)_L$	<b>2</b>	<b>1</b>	<b>2</b>	<b>2</b>	<b>3</b>	<b>1</b>
$U(1)_Y$	$-1/2$	$-1$	$-1/2$	$1/2$	$1$	$0$
$Z_2$	$+$	$+$	$-$	$+$	$-$	$-$



# Baroque Scotogenic Model

P.Čuljak, IP, K.Kumerički, PLB 744 (2015) 237

## Three-loop $R\nu$ MDM model



Yukawa interaction

$$\mathcal{L}_Y = -y_{e_i} \bar{L}_{iL} H_1 e_{iR} - Y_{i\alpha} \overline{(e_{iR})^c} \Phi^* \Sigma_{\alpha R} + \text{h.c.}$$

$\tilde{Z}_2$ -symmetric mixing quartic term

$$V_m(H_1, H_2, \Phi, \chi) = \kappa H_1 H_2 \Phi \chi + \text{h.c.}$$

# Exotic multiplets on top of 2HD

$$\Sigma_\alpha \sim (5, 0)$$

$$\Phi \sim (5, -2)$$

$$\chi \sim (7, 0)$$

$$\Sigma_{1111} = \Sigma_R^{++++}$$

$$\Phi_{1111} = \phi^+$$

$$\chi_{111111} = \chi^{++++}$$

$$\Sigma_{1112} = \frac{1}{\sqrt{4}} \Sigma_R^+$$

$$\Phi_{1112} = \frac{1}{\sqrt{4}} \phi^0$$

$$\chi_{211111} = \frac{1}{\sqrt{6}} \chi^{++}$$

$$\Sigma_{1122} = \frac{1}{\sqrt{6}} \Sigma_R^0$$

$$\Phi_{1122} = \frac{1}{\sqrt{6}} \phi^-$$

$$\chi_{221111} = \frac{1}{\sqrt{15}} \chi^+$$

$$\Sigma_{1222} = \frac{1}{\sqrt{4}} (\Sigma_L^+)^c$$

$$\Phi_{1222} = \frac{1}{\sqrt{4}} \phi^{--}$$

$$\chi_{222111} = \frac{1}{2\sqrt{5}} \chi^0$$

$$\Sigma_{2222} = (\Sigma_L^{++})^c,$$

$$\Phi_{2222} = \phi^{----},$$

$$\chi_{222211} = \frac{1}{\sqrt{15}} \chi^-$$

$$\chi_{222221} = \frac{1}{\sqrt{6}} \chi^{--}$$

$$\chi_{222222} = \chi^{----},$$

# Accidental DM protecting symmetry

dimension-three  $Z_2$ -noninvariant operator

$$\mu\Phi\Phi^*\chi$$

is forbidden by the  $\tilde{Z}_2$  symmetry enforced on the 2HD sector

$$(H_1, H_2) \rightarrow (H_1, -H_2)$$

In the “lepton-specific” (Type X or Type IV) model

$H_2$  couples to all quarks whereas  $H_1$  couples to all leptons

	$Q_i$	$u_{iR}$	$d_{iR}$	$L_{iL}$	$e_{iR}$	$H_1$	$H_2$	$\Phi$	$\chi$	$\Sigma_\alpha$
$Z_2$ accidental	+	+	+	+	+	+	+	-	-	-
$\tilde{Z}_2$ exact, imposed	+	-	-	+	+	+	-	+	-	+

# Conclusions:

- Diphoton excess (if confirmed) is in favour of a setup which is appropriate for Radiative Neutrino Models (minimal or baroque):
- Triplet  $Y=0$  scalar which mixes with SM Higgs
- Triplets ( $Y=0$  and/or 2) which are constrained by imposing loop- or DM protecting  $Z_2$  symmetry
- Conceivable scenarios with automatic dark  $Z_2$  symmetry - an example of fermion quintuplet Majorana DM candidate with mass  $< 450$  GeV discoverable using monojet searches @HL-LHC
- Diphoton and other measured signals may help to discriminate between different scenarios