

UiO : **Department of Physics**  
University of Oslo

# Thermoelectric Phenomena and Bulk and Interface Transport

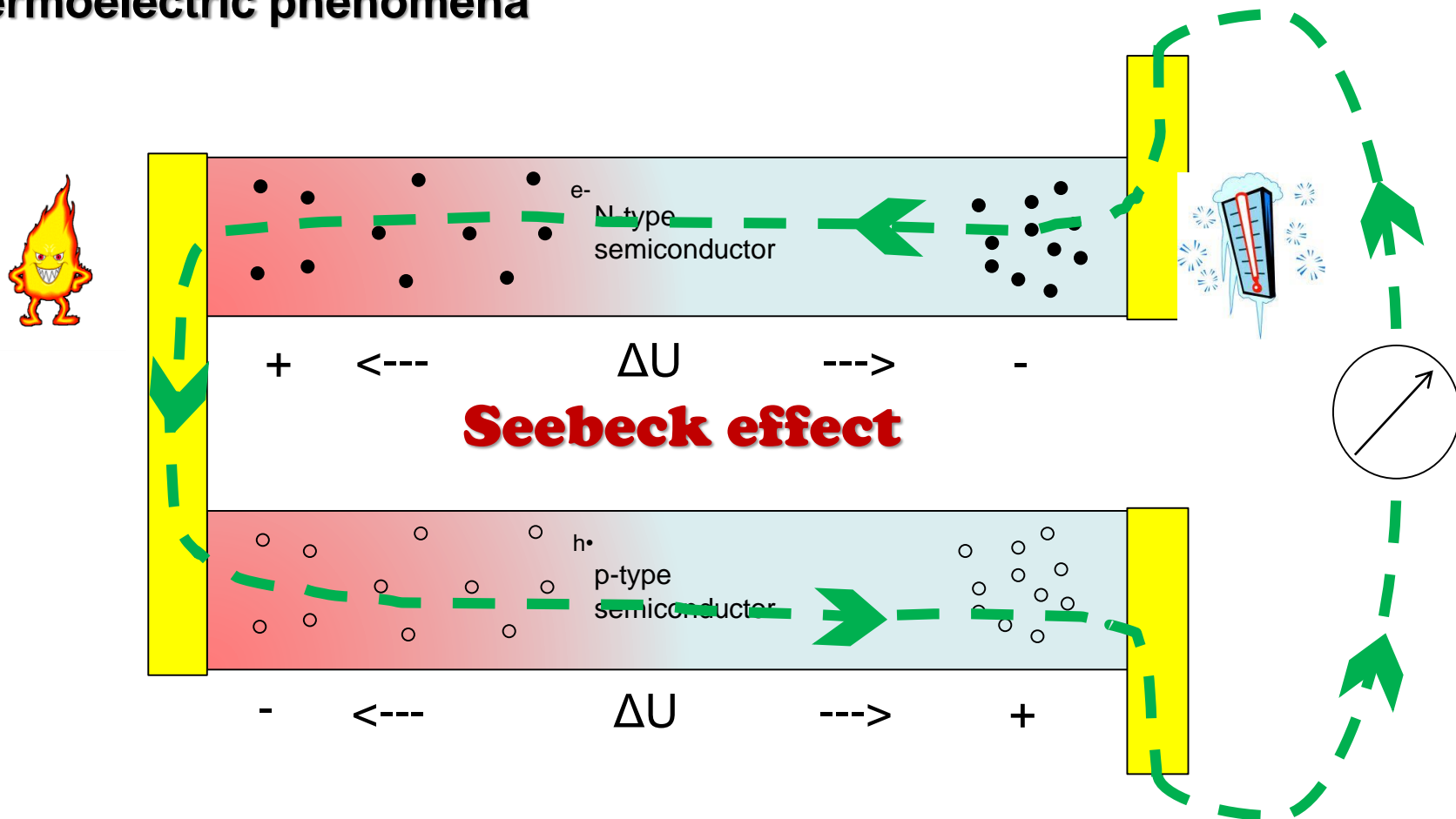


Xin Song  
Postdoc.  
Dep. Physics, University of Oslo

## Outline:

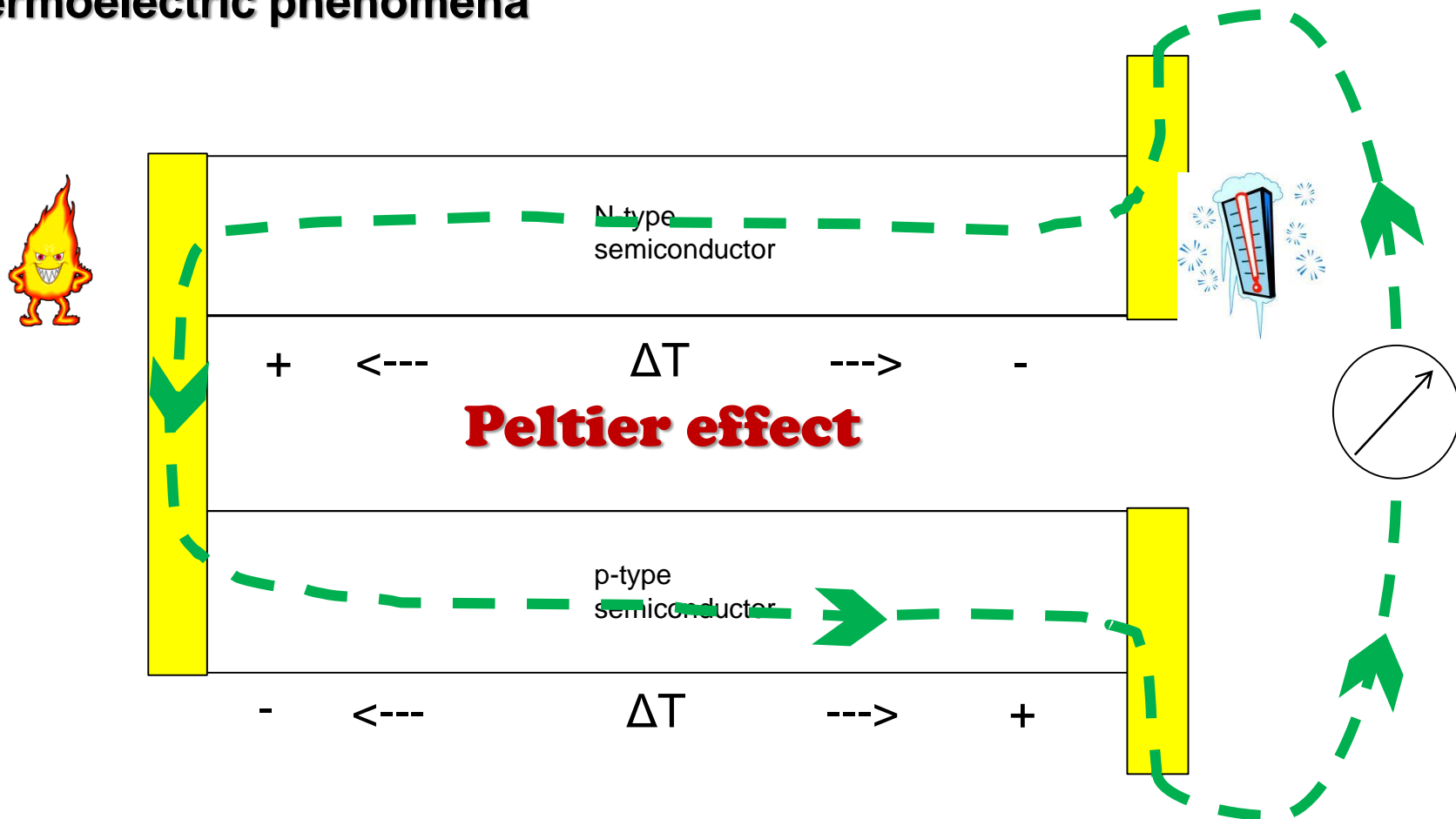
- **Bulk transport** – two approaches  
Laudauer approach – illustrative for phenomena  
BTE – descriptive for correlations in transport
- **Transport at interface**

## Thermoelectric phenomena



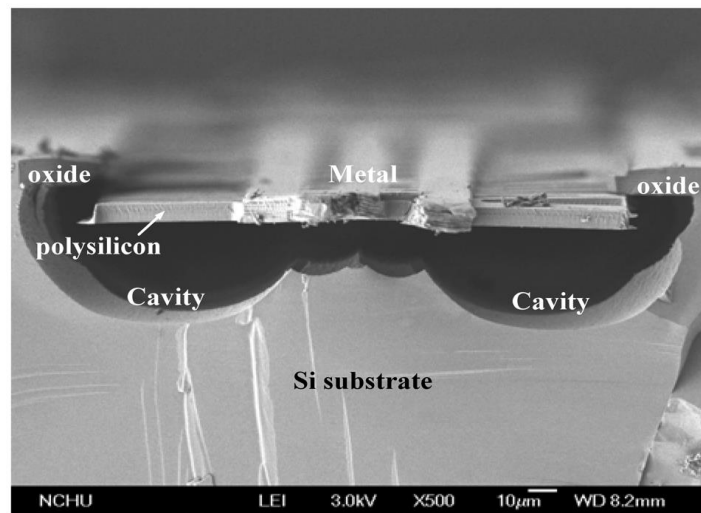
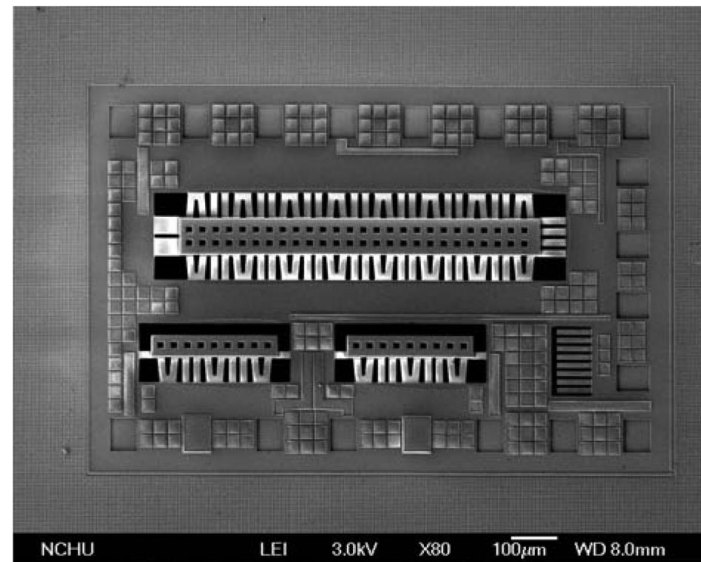
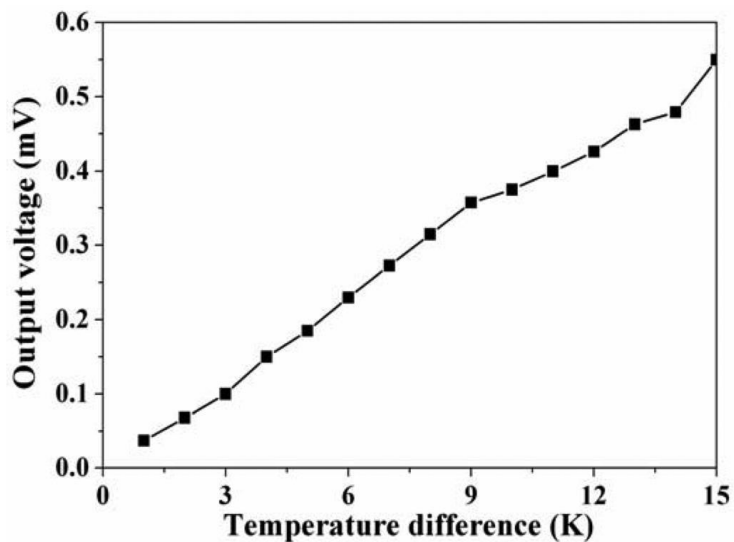
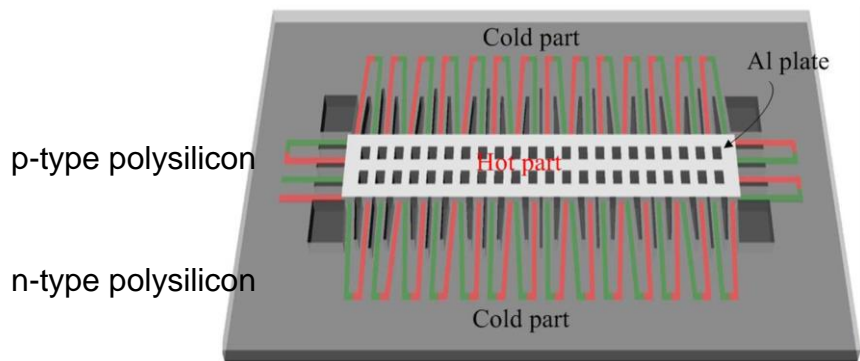
Thermoelectric circuit

## Thermoelectric phenomena

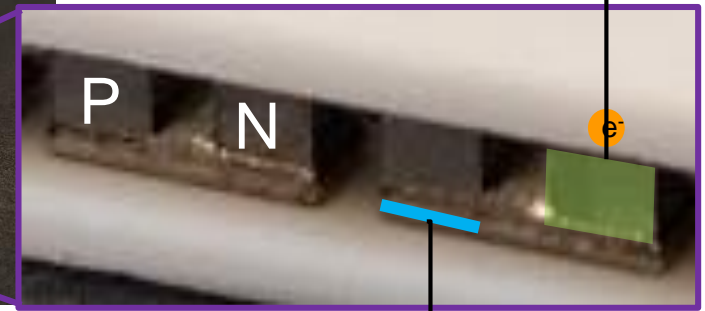
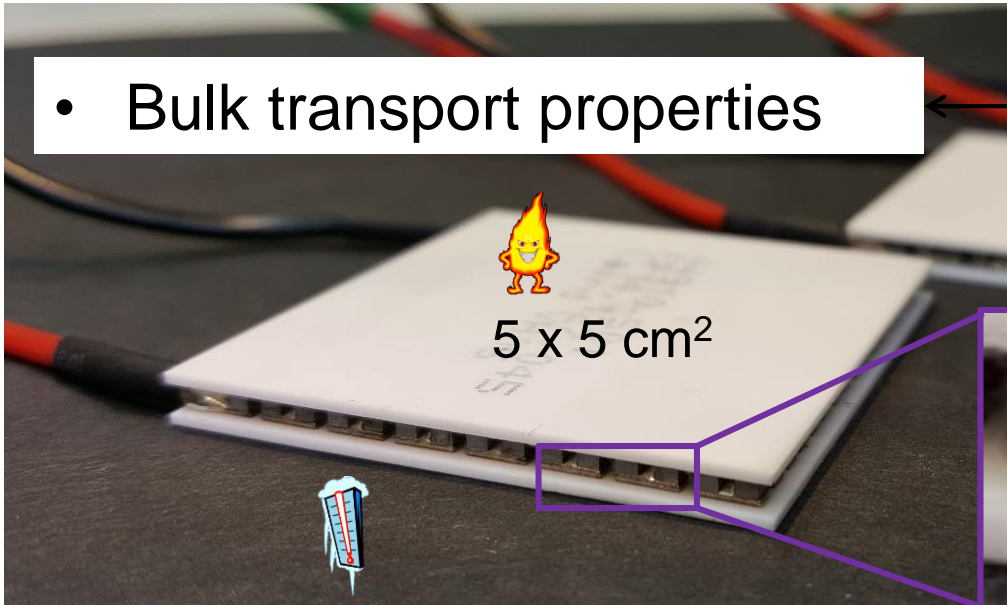


Thermoelectric circuit

## MEMS thermoelectric generator

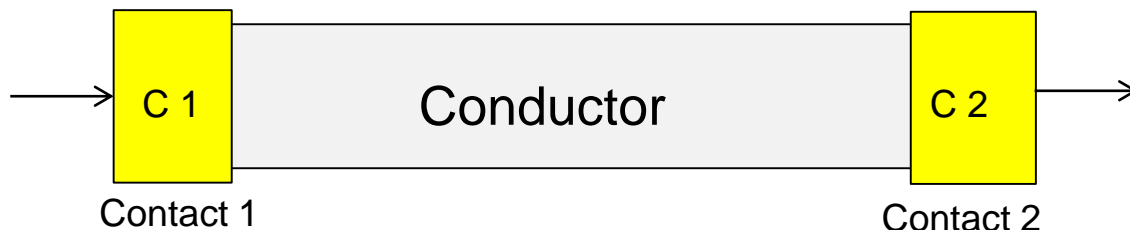


- Bulk transport properties

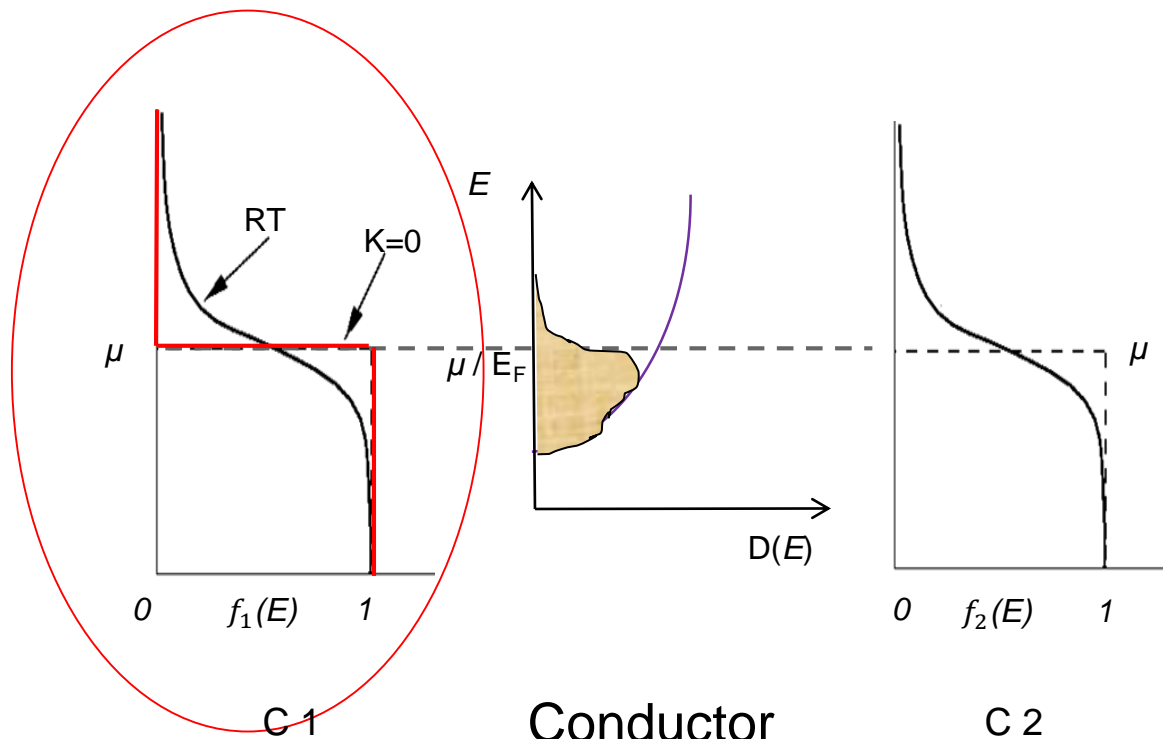


- Interface transport properties

- Bulk transport properties
  - **Landauer approach – Thermoelectric phenomena**  
Ballistic transport;  
Approximate but illustrative.
  - **Boltzmann transport equations – transport coefficients**  
Diffusive transport;  
Statistical behaviour, relatively closer to reality, but **realitively**;  
Correlation of transport coefficients.



- Equilibrium, no external force



Fermi Distribution

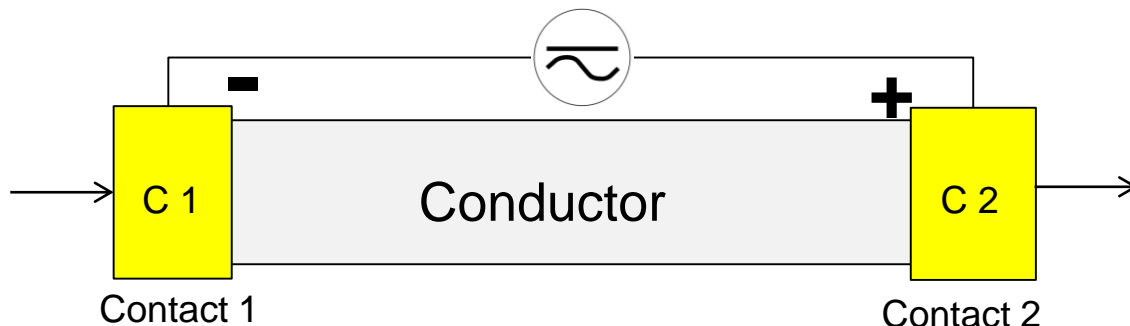
$$I = G\Delta V + G_S\Delta T$$

$\swarrow$                        $\searrow$   
 Ohmic                      Seebeck  
 current                      current

$$\begin{aligned}
 \left. \begin{matrix} G \\ G_S \end{matrix} \right\} &\propto A \int D(E)(f_1 - f_2) \\
 &\propto \int D(E) \left( -\frac{\partial f_0}{\partial E} \right)
 \end{aligned}$$

No net current

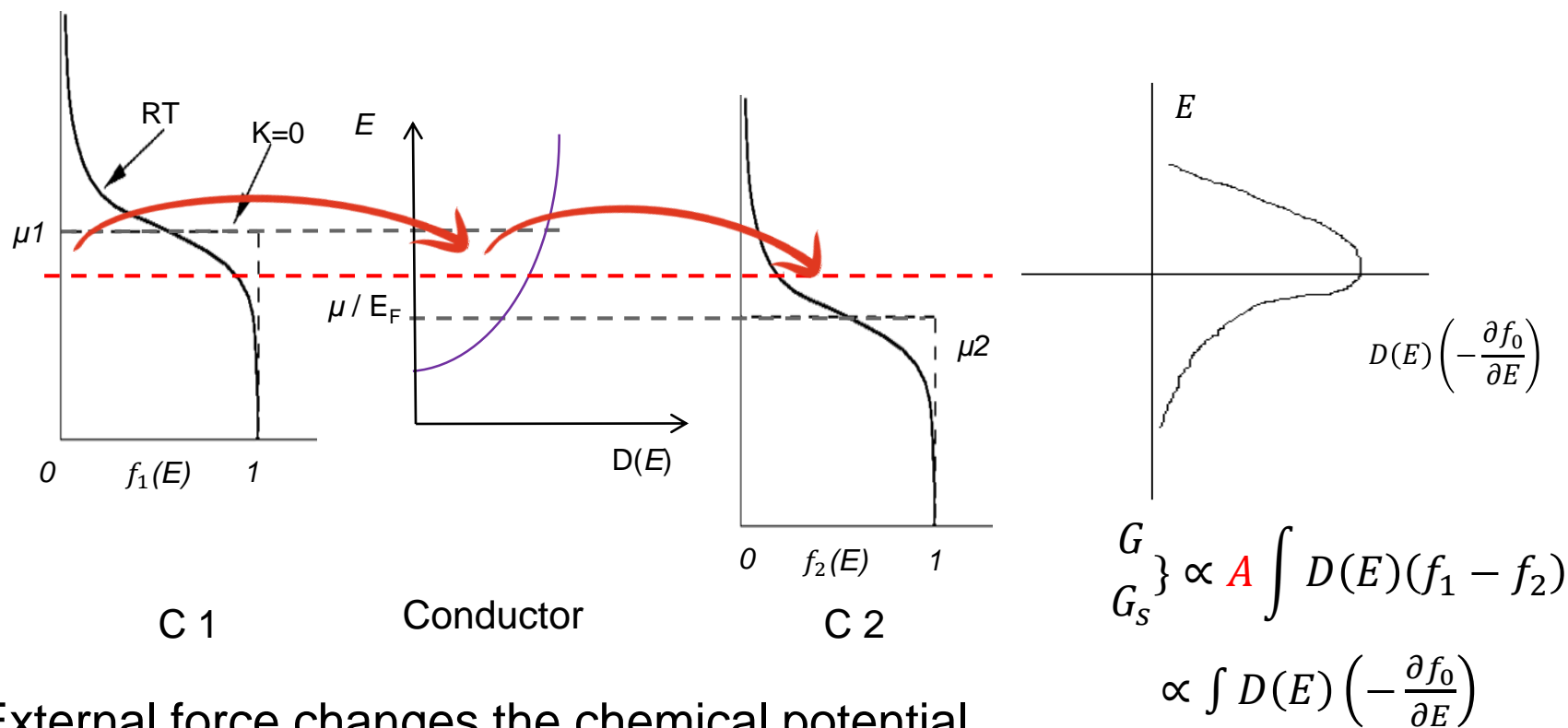




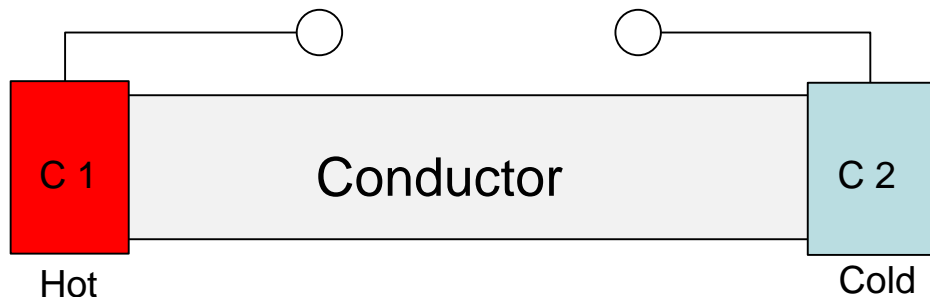
$$I = G\Delta V + \cancel{S\Delta T}$$

↓ Ohmic current      ↓ Seebeck current

- When apply electric force



External force changes the chemical potential

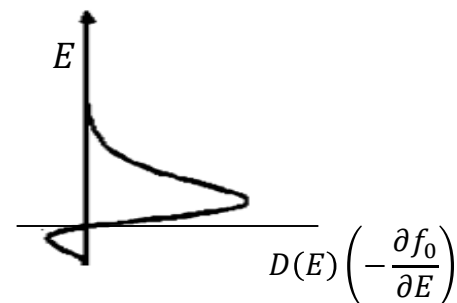
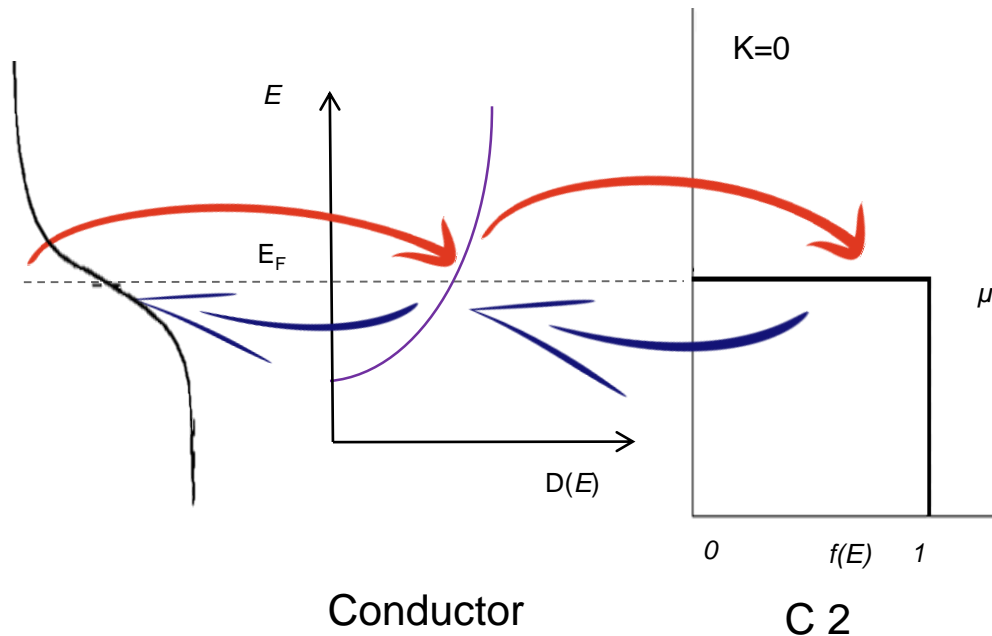


$$I = G\Delta V + G_S\Delta T$$

$$\Delta V = \cancel{\frac{I}{G}} + \left(\frac{G_S}{G}\right)\Delta T$$

Seebeck coefficient

- When apply temperature difference on an open circuit

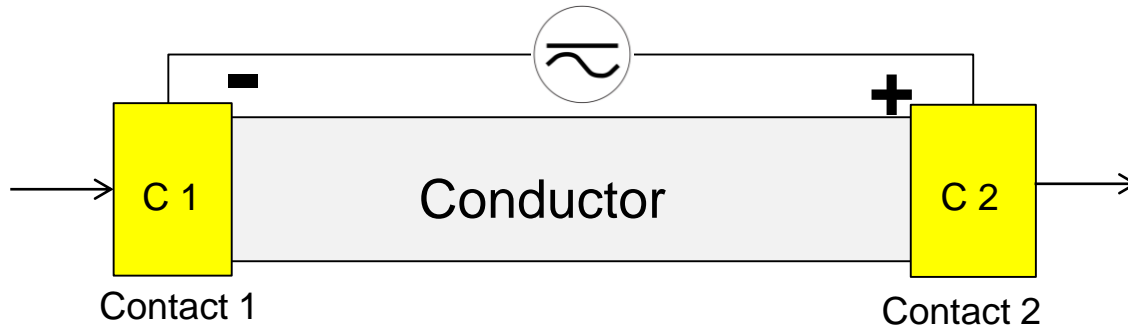


$$\left. \begin{matrix} G \\ G_S \end{matrix} \right\} \propto A \int D(E)(f_1 - f_2)$$

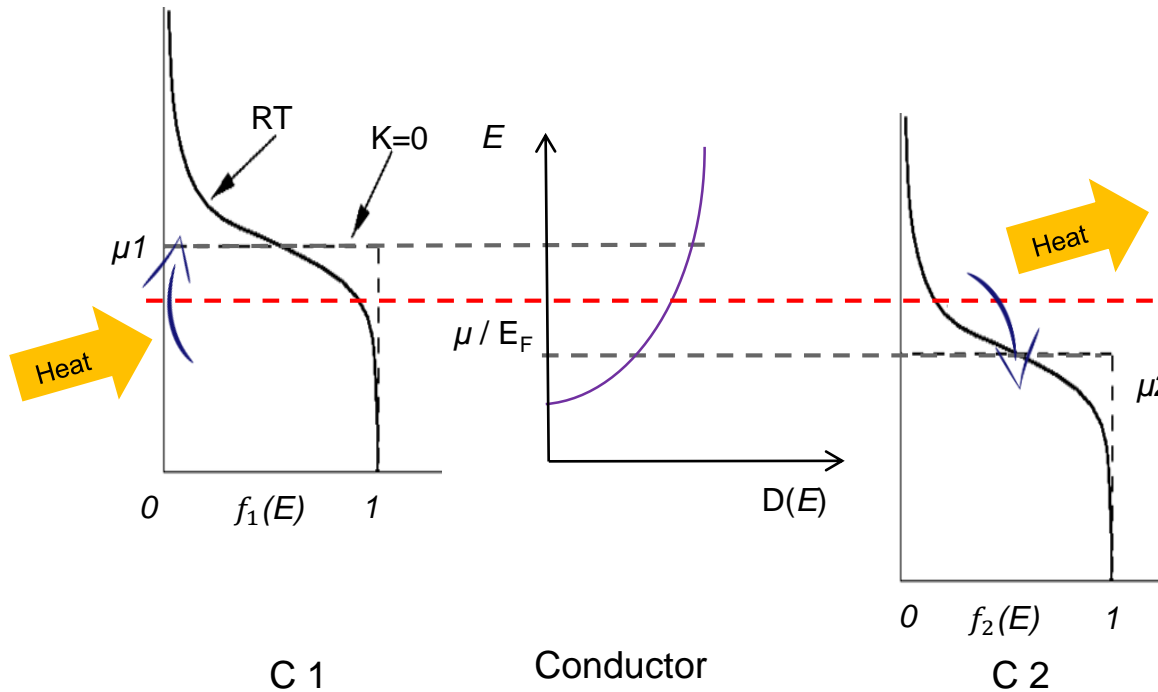
$$\propto \int D(E) \left( -\frac{\partial f_0}{\partial E} \right)$$

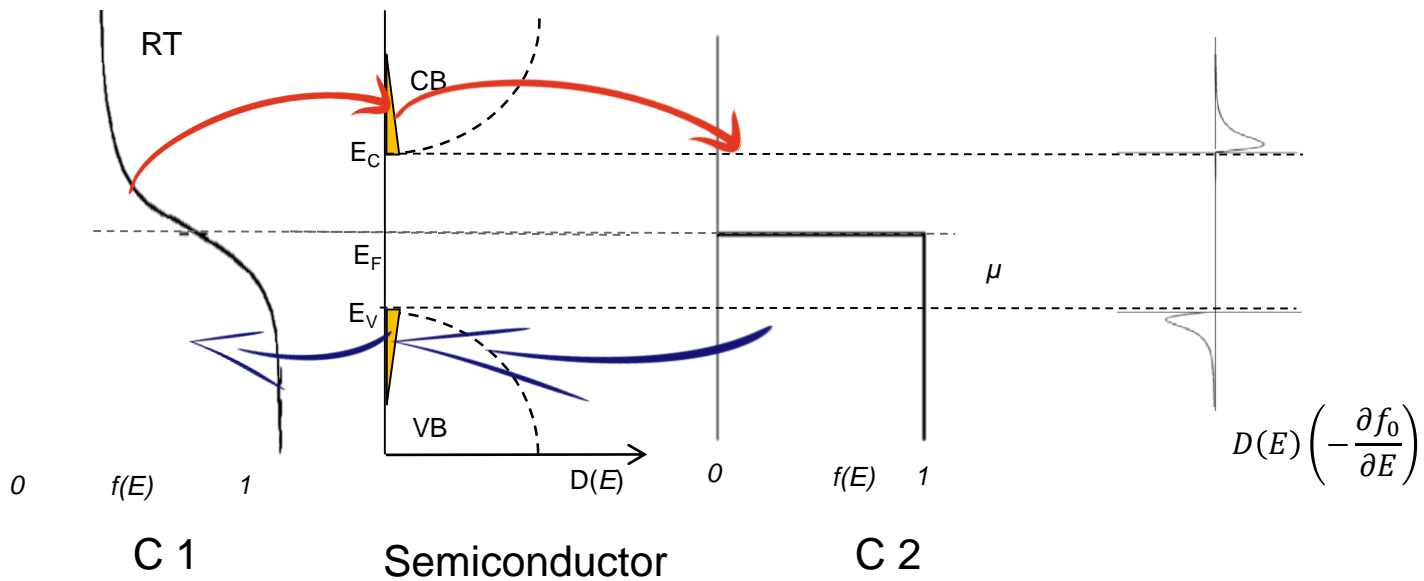
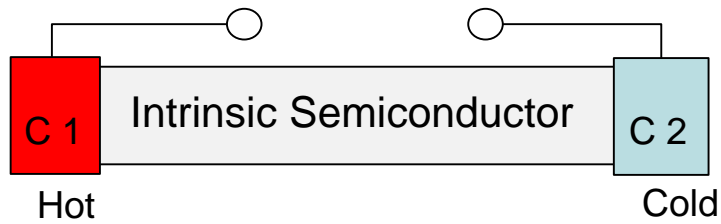
Temperature difference changes charge Fermi distribution

$$A = \begin{cases} 1 & \text{for } G \\ \frac{E - \mu}{qT} & \text{for } G_S \end{cases}$$

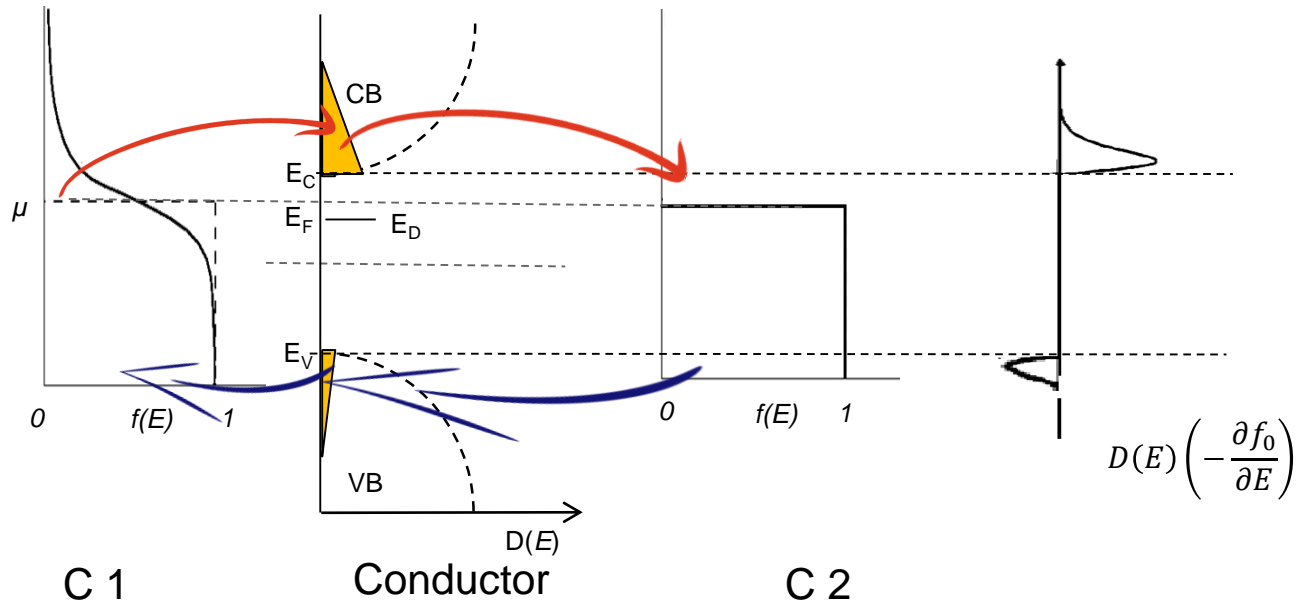
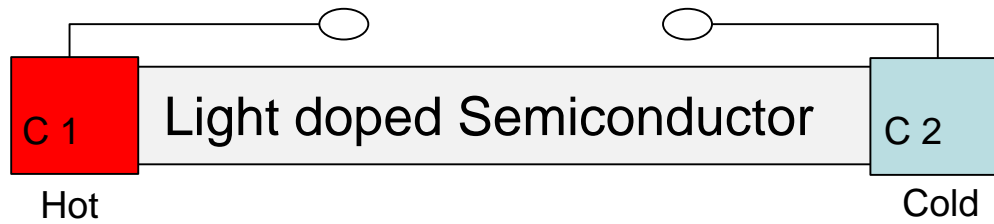


- Peltier effect

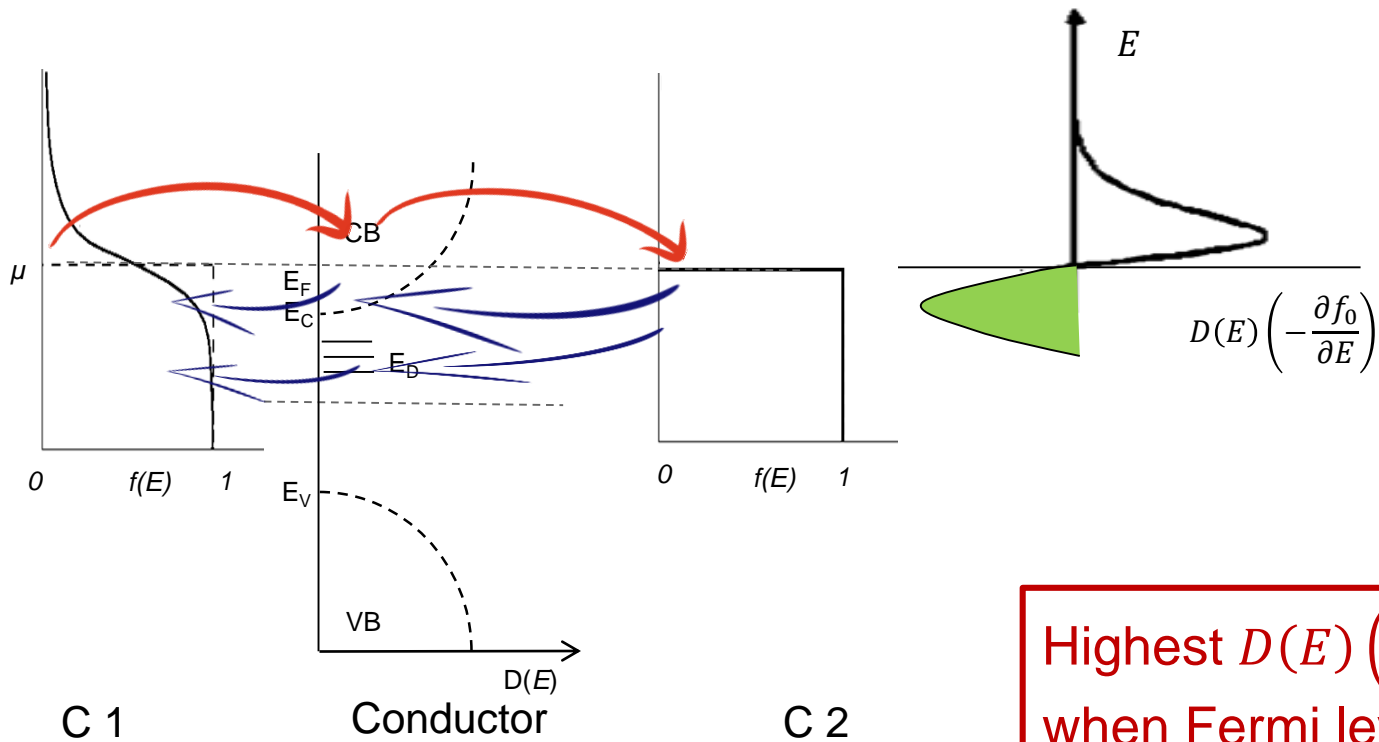
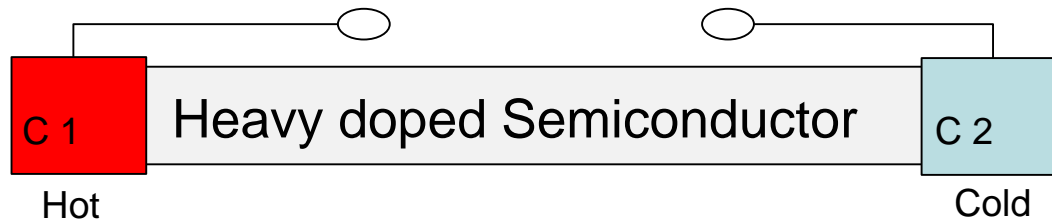




Intrinsic semiconductor has zero seebeck

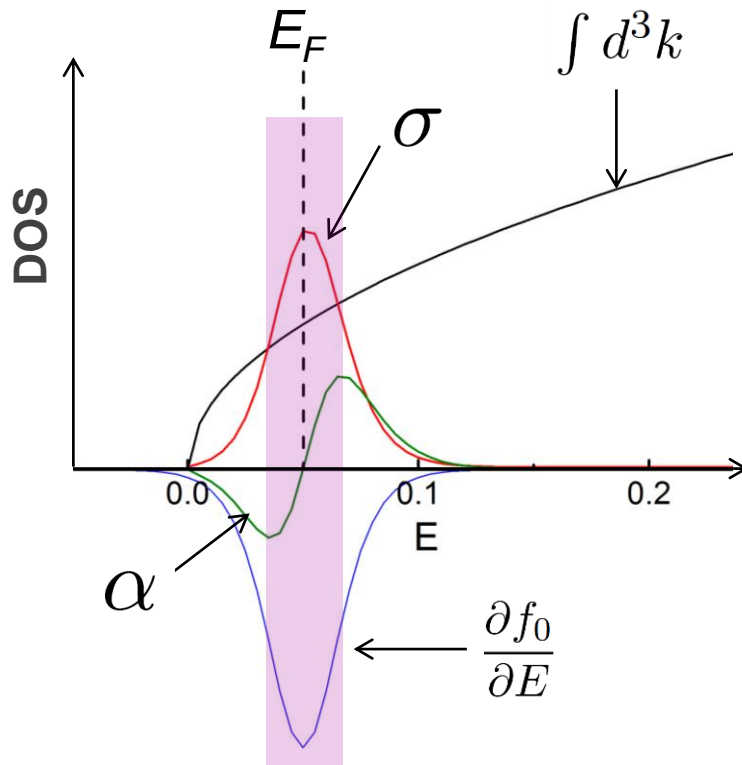


Asymmetric DOS -> higher Seebeck



Highest  $D(E) \left( -\frac{\partial f_0}{\partial E} \right)$  occurs when Fermi level is close to band edge.

- Optimizing power factor



Seebeck coefficient

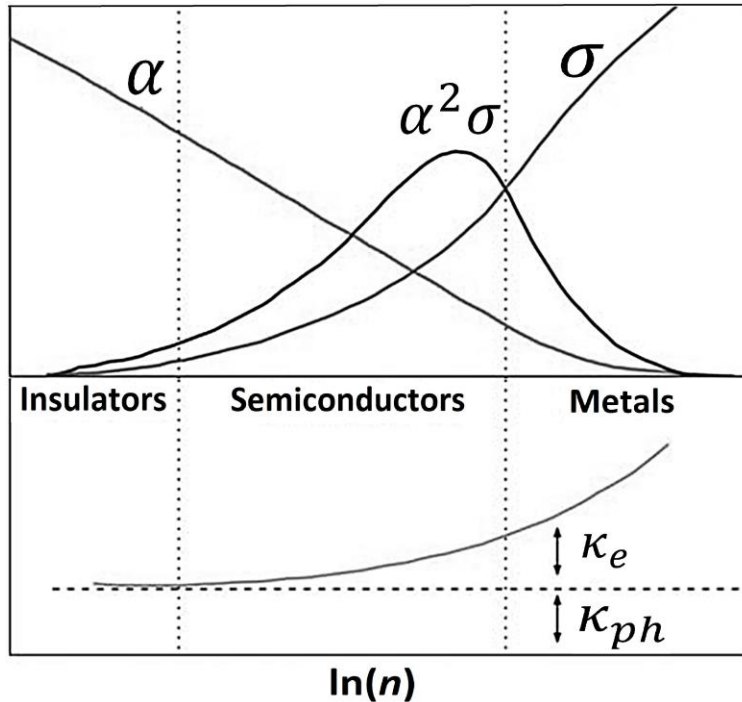
$$\alpha = \frac{1}{qT} \frac{\int \tau v^2 (E - E_F) \left(-\frac{\partial f_0}{\partial E}\right) d^3k}{\int \tau v^2 \left(-\frac{\partial f_0}{\partial E}\right) d^3k}$$

Electrical conductivity

$$\sigma = \frac{q^2}{4\pi^3} \int \tau v^2 \left(-\frac{\partial f_0}{\partial E}\right) d^3k$$

$$zT = \frac{\alpha^2 \sigma}{\kappa_e + \kappa_{ph}} T$$

- Optimizing power factor



- Optimize the interaction between transport coefficients
- Doping, defect scattering, energy filtering

Seebeck coefficient

$$\alpha = \frac{8\pi^2 k_B^2}{3qh^2} m^* T \left( \frac{\pi}{3n} \right)^{2/3}$$

Electrical conductivity

$$\sigma = qn \left( \frac{q\tau}{m^*} \right)$$

$$zT = \frac{\alpha^2 \sigma}{\kappa_e + \kappa_{ph}} T$$

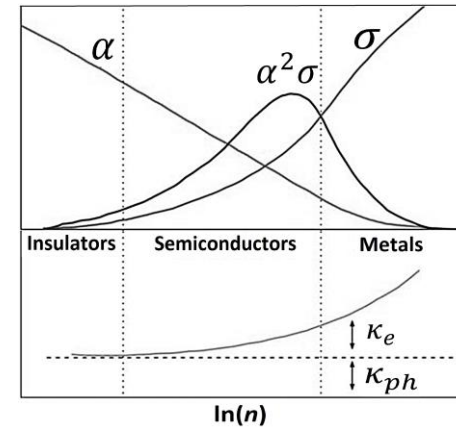
Wiedemann-Franz law

$$\kappa_e = nq\mu\mathcal{L}T$$



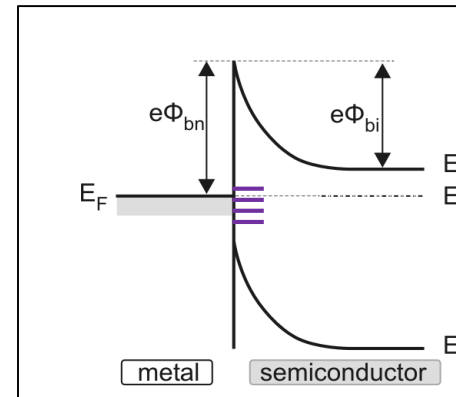
- Bulk transport properties

- How much electrons/ holes,  $\alpha$ ,  $n$
- The ability electrons/ holes move,  $\sigma$ ,  $\mu$ ,  $n$
- The ability heat propagate,  $\kappa$
- Expect  $zT > 1$



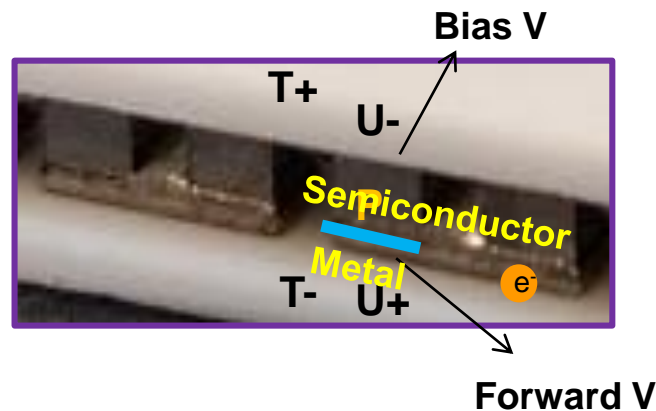
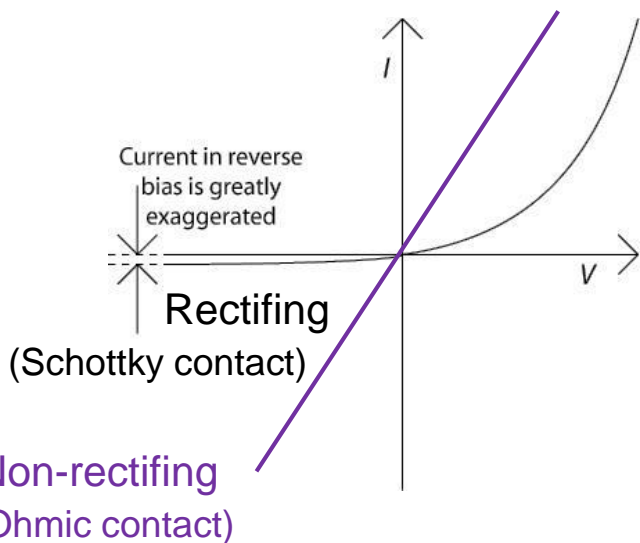
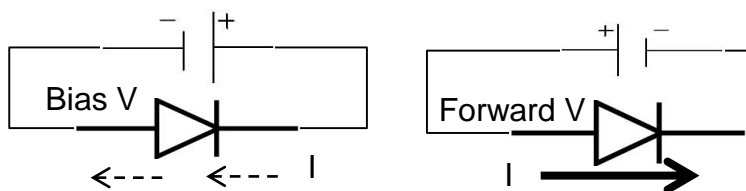
- Interface transport properties

- Non-rectifying contact
- Rectifying contact,  $R_C$
- Interface states,  $N_a$

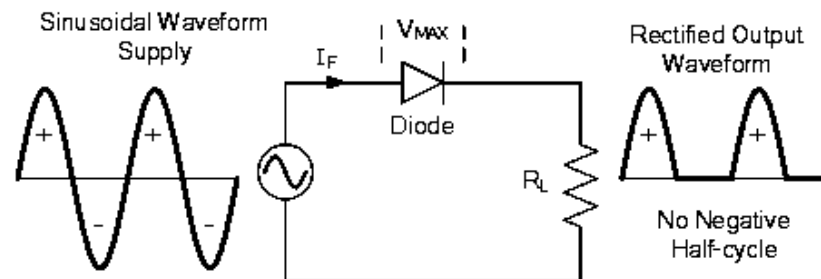


# Interface transport properties

## Rectification



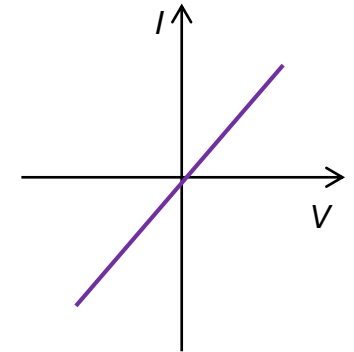
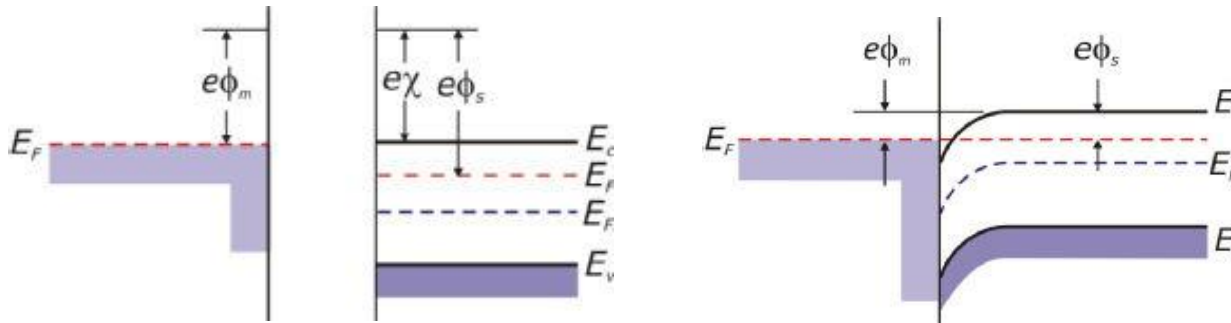
High contact resistance  $R_C$  !!



## Interface transport properties

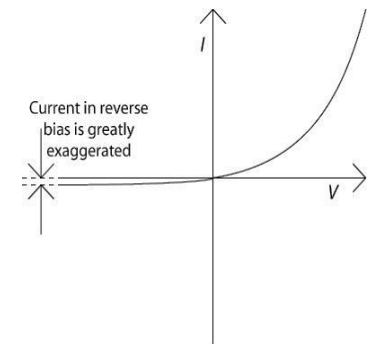
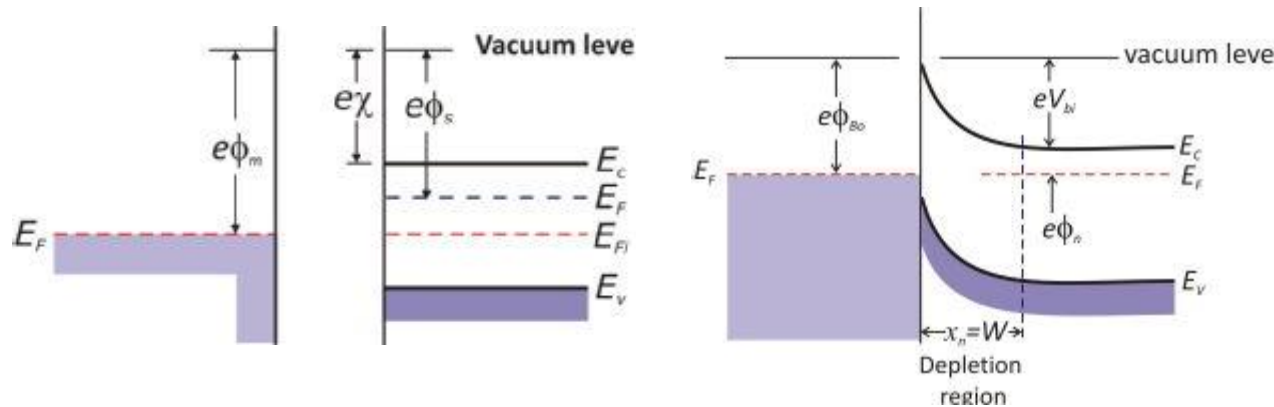
The ideal non-rectifying barriers (Ohmic contact)

Metal work function  $\phi_m \approx$  Semiconductor electron affinity  $\chi$



Rectifying barriers (Schottky contact)

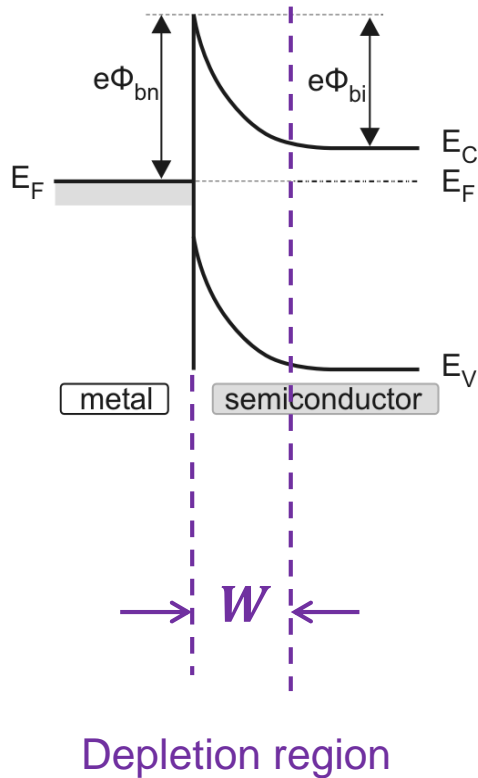
Metal work function  $\phi_m \gg$  Semiconductor electron affinity  $\chi$



Barrier height  $\phi_{b0} = \phi_m - \chi$

# Interface transport properties

## The Tunneling Barriers



$$W = \sqrt{\frac{2\epsilon_s(e\phi_{bi} + V - \frac{kT}{e})}{eN_d}}$$

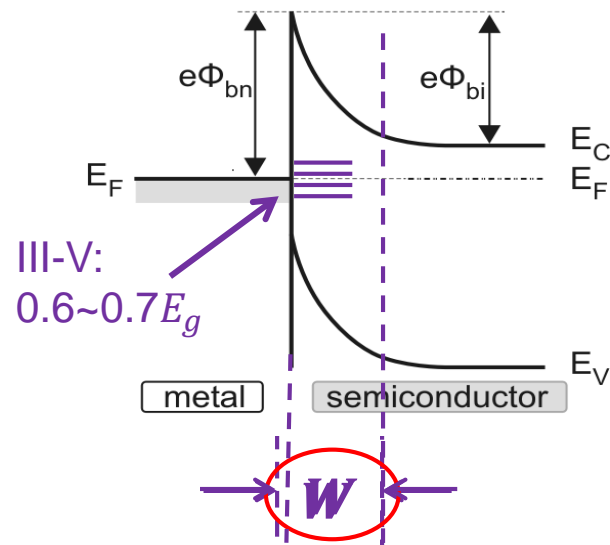
- $\epsilon_s$  -- Dielectric constant -- Fixed
- $e\phi_{bi}$  -- Built-in potential -- Fixed
- $N_d$  -- Doping concentration -- Manipulative ☺

For most semiconductors

<p>(a) Thermionic emission</p>	<p>Schottky</p>	$N_d < 10^{17} \text{ cm}^{-3}$
<p>(b) Thermionic-field emission</p>		$N_d = 10^{17} \sim 10^{18} \text{ cm}^{-3}$
<p>(c) Field emission.</p>	<p>Ohmic</p>	$N_d = 10^{19} \sim 10^{20} \text{ cm}^{-3}$ $W$ small enough for tunneling

## Interface transport properties

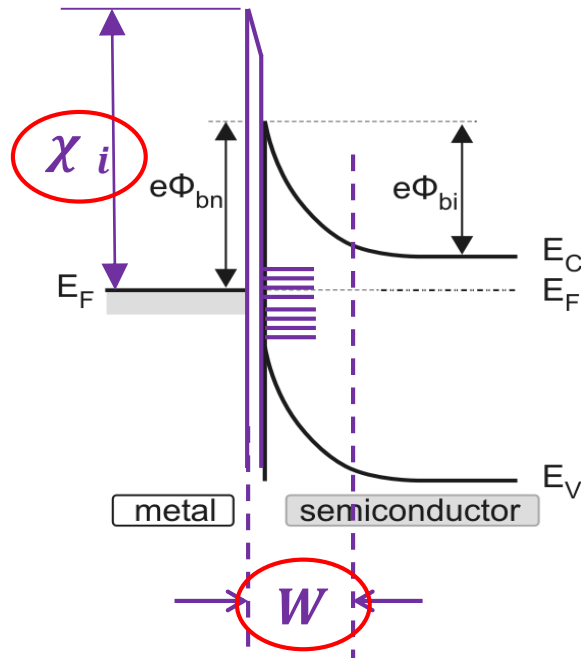
### More complicated- interface states in reality



- Pinning the Fermi level
- High density of surface states  
→ Dielectric barrier  $\chi_i$ , dominating!
- In real world, M-S interface is about
  - Selection of metal
  - Epitaxial growth

## Interface transport properties

### More complicated- interface states in reality



- Pinning the Fermi level
- High density of surface states  
→ Dielectric barrier  $\chi_i$ , dominating!
- In real world, M-S interface is about
  - Selection of metal
  - Epitaxial growth

Sum up:

- **Bulk transport – two approaches**

Laudauer approach – illustrative for phenomena

BTE – descriptive for correlations between  $\alpha$ ,  $n$ ,  $\sigma$ ,  $\mu$ ,  $\kappa$

- **Transport at interface**

Non-rectifying contact

I need learn more from you